



Environment
Canada

Environnement
Canada

Canada

The Use of GPSRO data at Environment Canada

ROM SAF Workshop

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Overview

- History & current status at Environment Canada (EC)
 - Assimilated data, assimilation details
- Philosophical & engineering choices
 - Rationale
 - Trade-offs
 - Performance
- Overview of items under development
 - Low atmosphere
 - Boundary layer
 - Surface reflections
 - Horizontal gradients



History

- 2003: Begins development.
- 2004-06: Tests for different architectures
- 2007: Final structure, philosophy, settled (Refr & BA)
- 2008: Op readiness, 1st delivered implementation (Refr).
- 2009: Op production (Refr, model lid 10 hPa, 30 km)
- 2010: Vertical extension (Refr, model lid 0.1 hPa, 65 km)
- 2011: Reevaluation of physical constitutive relations
- 2013: Reimplementation with updated physics
- 2014: New BA, reflection-aware
 - Still assimilating Refr
- 2015: Activate BA & reflections? Partial activation?



Perspective: Cost function

- Variational assimilation (Bayesian optimization)
 - At EC we also have Ensemble assimilation
- Variational: Minimize departure from knowledge (x_B and O)
 - $J = J_B + J_O = \frac{1}{2} (x - x_B)^T B (x - x_B) + \frac{1}{2} \left(\frac{O - H(x)}{\sigma} \right)^2$
 - Find max probability = min cost function
 - 3DVar / 4DVar / EnKF / EnVar versions of the concept
- Variational or ensemble we need defined by
 - List of data (N or Bend, rejection criteria) *user, on provider spec*
 - **H(x)** function *user, on provider spec*
 - σ for each datum *now is user*
***should** be provider*



Who should provide what:

- B (estimated background covariance) NWP system
- H(x) obs operator user optimal choice:
H conceptually based on instrument & processing (provider-side), but x is a NWP-dependent **imperfect** representation of atmosphere (incomplete, discretized,...)
- Data choice user optimal: (NWP **sensitivity** to obs errors/bias)
- σ Obs error, or also covariance: **provider** (now is user)



Early choices at EC

- From **datum**-oriented cost function:

- $$J_O = \sum_1^{nObs} \left(\frac{O-H(x)}{\sigma} \right)^2$$

- To **profile**-oriented

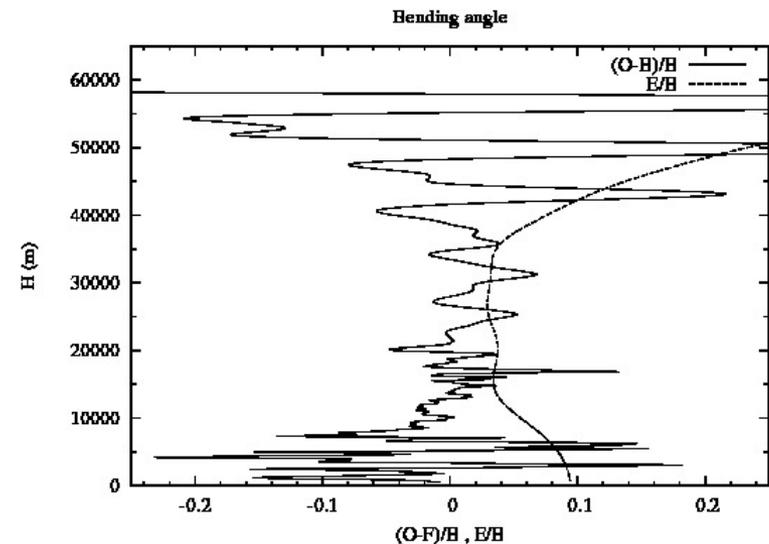
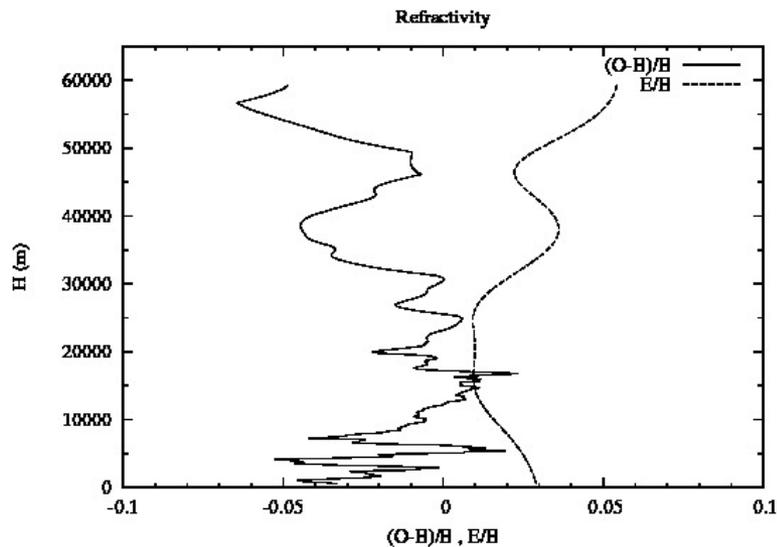
- $$J_O = \sum_1^{nProf} \sum_1^{nData} \left(\frac{O-H(x)}{\sigma} \right)^2 = \sum_1^{nProf} f(x; \vec{O})$$

- We assume that data naturally show collective properties by **profile** (not by datum / satellite / ...)
- Rationale: data have been collected & processed as profiles, any anomaly will emerge collectively (orbit error, ionosphere...)



The profile cost function

- How much is the observation error σ ?
 - Very variable by instrument, inversion, circumstances, atmosphere state.
 - Some hint by providers, but still very uneven, not always offered.
- We determine our own:
- Window (5 km Gaussian) vertical rms avg of $\frac{O-H(x)}{H(x)}$ is taken as $\frac{\sigma}{H(x)}$



Profile-oriented obs error

- Valid when actual error too unknown
- Maybe not optimal, but **not too small, not too big**
- Will **dynamically** respond to transient orbit / iono error

- If obs was genuinely of bad quality
 - Err will be big (bad data ignored, ok!)
- If background was of bad quality
 - Err will be big (good data ignored, but can we expect good assimilation behavior of complex vertical info over bad bg?)
- Has naturally evolved with the providers' retrieval and NWP system (**2006-2014**) without recalibration
 - UTLS err evolved from 2% to 0.6%.

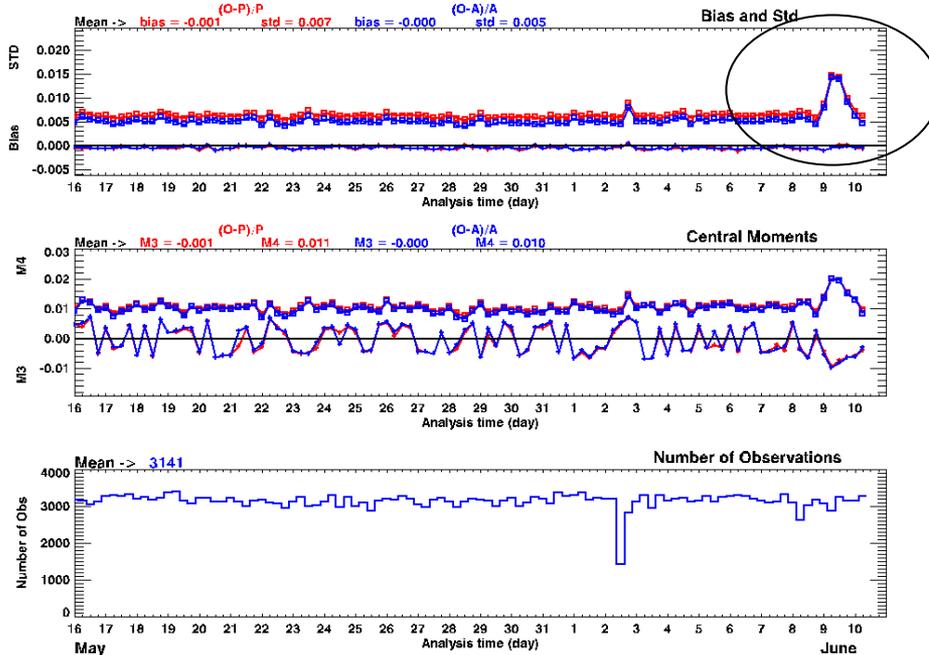


Dynamic error adjustment

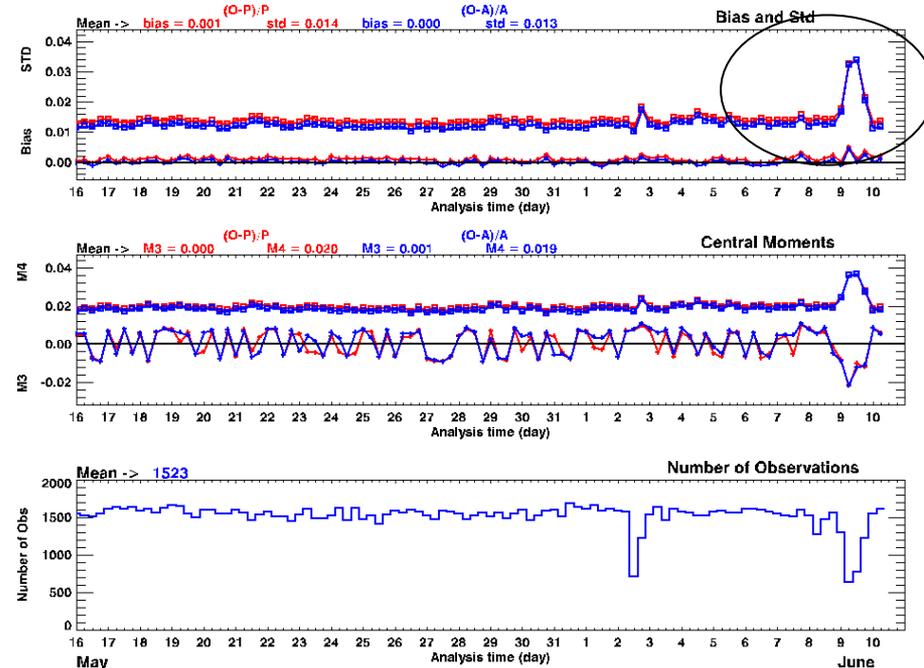
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Error was dynamically raised, and analysis mostly ignored unflagged biased data
 O-A stats = O-P stats

Date = 2014061006 GPSRO Observations: METOP-2 Levels 10 - 30km



Date = 2014061006 GPSRO Observations: METOP-2 Levels 30 - 40km



Choice of data at EC

- 1st test (2006+): Refractivity
 - Model lid was 10 hPa (~30 km)
 - Became operational Mar 2009 with 10 hPa lid
 - Operational lid raised in Jun 2009 (0.1 hPa, ~65 km)
 - Only deterministic NWP was 0.1 hPa
 - Ensemble system has low lid (now 2 hPa, ~45 km)
 - Both share data, checks, bias correction, thinning.
 - **Lid limited choice of BA**
- 2nd test (2012): Bending recoding
 - Nice results from deterministic system
 - Good short term, lower bias, can consider reflections
 - **(bend+error) does NOT beat our (refrac+err) at mid & long range**
- **Research line: Mixed**
 - Unquestionable benefits from BA
 - Some benefits from Refr too



Is Refractivity so bad?

- **Providers:**

- Phase → Doppler → Bending → Refractivity
- Deprojection integral (Abel) discretized in ~**5000** points
- Numerical interpolation **not critical**

$$\frac{n(r)}{n(r_{max})} = \exp\left(\frac{1}{\pi} \int_x^{x_{max}} \frac{\alpha(a)}{\sqrt{a^2 - x^2}} da\right)$$

Notice integral does not need to be extended to infinity, if we accept a ratio of n (~diff of N) rather than n itself

- **Users:**

- P, T, q fields → Refractivity → Bending
- Projection integral (Abel) discretized in ~**50-100** points (81 at EC)
 - Or equivalent integral in 2d/3d operator
- Numerical interpolation **critical** (not always accurate)

$$\alpha(a) = -2a \int_a^{\infty} \frac{d \ln n / dx}{\sqrt{x^2 - a^2}} dx$$



Pro & con

- Providers better positioned than users to perform “Abel-like” integrals
 - small scale information representable in bending obs but at the edge of model resolution (**nontrivial to assimilate**)
 - Refractivity, as a cumulative, can inject info at the required resolution
- About upper initialization (i.e. climate): We should NOT assume that we obtain

$$N(h) \qquad \int f(x)dx + C$$

but instead

$$N(h_1) - N(h_2) \qquad \int_x^{top} f(x)dx$$

where $h_2 < \infty$

- We **should** in general understand “refractivity info” as **refractivity increments**, not **absolute refractivity**.
- Superrefraction, low level structure
- Abel retrieval does **not** represent reflection



Physical basis of the operators

- Equation of state
- Thermodynamic expression of refractivity
- Earth's geometry
- Interpolation in the discretized grid
- Refraction & reflection



Locality of operators

- Measurement is $N(h)$ or $\alpha(a)$
 - h or a are expressions of location \vec{x}
- Must be interpreted as fields of P, T, q
- Required
 - Refractivity expression $N \leftrightarrow P, T, q$
Local relationship (thermodynamic)
 - Geometric structure of the atmosphere $\vec{x} \leftrightarrow P, T, q$
Nonlocal (hydrostatic eqn, etc)

Even $N(h)$ is nonlocal

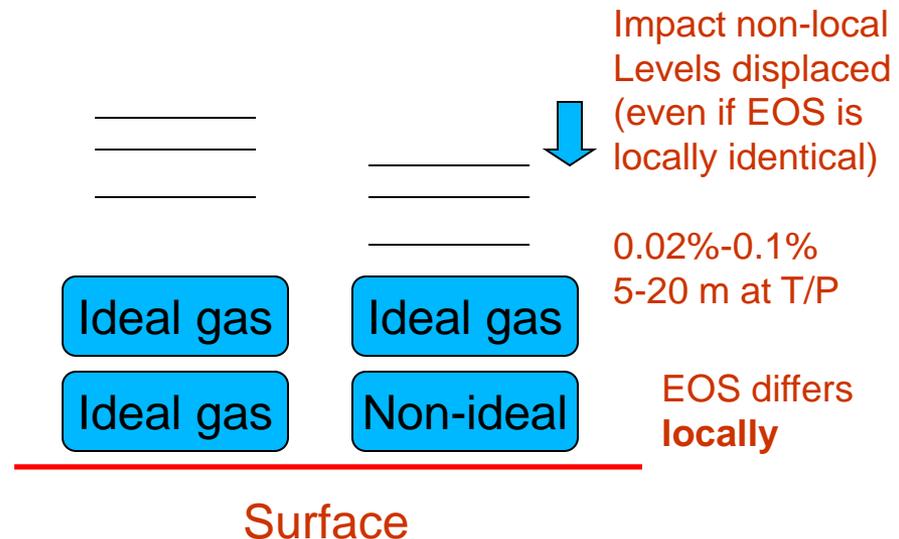


Equation of state

- We assume hydrostatic equilibrium
- We need there the equation of state (EOS)
- Found that the deviation of EOS from ideal is small but non-negligible
- **Non-local**
- 0.05%, which is relevant for NWP if **systematic** (affects the anchor of radiances)

$$\nabla P = -\vec{g}(\vec{x})\rho$$

$$P(\rho, T, x_w)$$



Earth's geometry

- **We know the following to be relevant for RO**
 - Earth is not spherical
 - Local curvature depends on lat, azimuth
 - Mean sea level (~geoid) shape
 - Strength of gravity varies with latitude and altitude
- **We assume**
 - Shape of WGS84
 - Curvature, strength of gravity (lat, alt)
 - Height of MSL over WGS84 as main equipotential surf in EGM96
- **We neglect**
 - Gravity anomaly (geoid-dependent, lat & lon)
 - Sea surface topography (sea temperature, dynamics or salinity)
 - Variation of MSL within an occultation



Setup at Env Canada

Hydrostatic equation $g(\lambda, h)$

- Should consider
- EOS should include compressibility $\rho(P, T, x_w)$

Refractivity expression

- Calibration should have included compressibility
- Expressions of the form $N = k_1 P_d / T + k_2 P_w / T + k_3 P_w / T^2$

cannot attain stated accuracy (for any set of coefficients)

- By theory or experiment should consider
 - Air composition
 - Molecular polarizability
 - Electric dipoles (H2O)
 - Magnetic (O2) dipoles
 - Dielectric enhancement
 - Univocal meaning

Proposal :

$$N = N_0(1 + N_0 \cdot 10^{-6} / 6)$$

$$N_0 = (222.682 + 0.069 \cdot \tau) \cdot \rho_d + (6701.605 + 6385.886 \cdot \tau) \cdot \rho_w$$

$$\tau = 273.15 / T - 1$$



Dry air refractivity

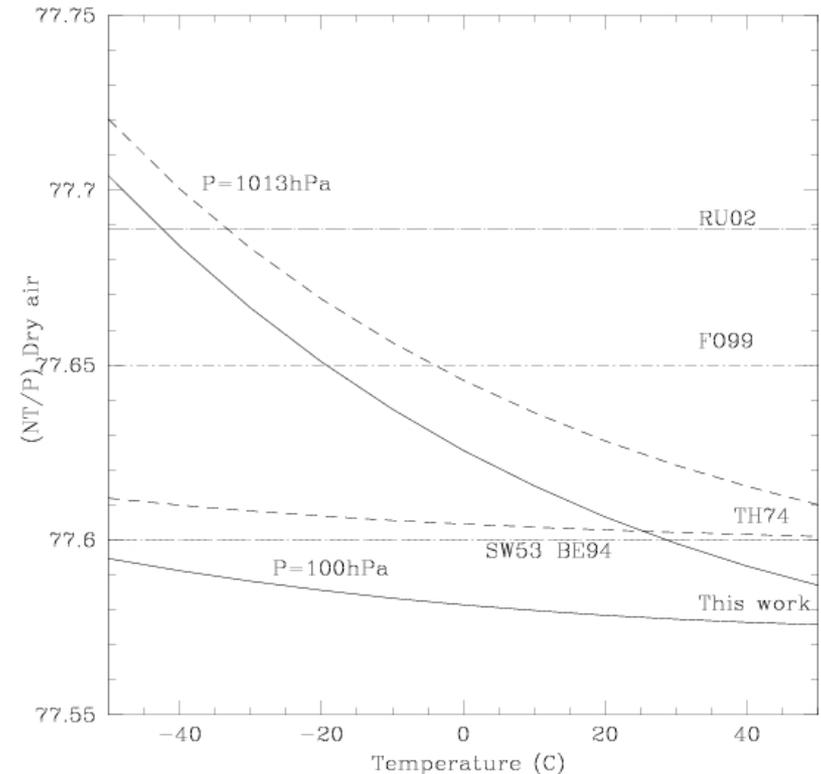
What is normally called
 k_1 (NT/P for dry air)

Not a constant

No constant would fit to
better than 0.1% rms
(max err up to 0.2%)

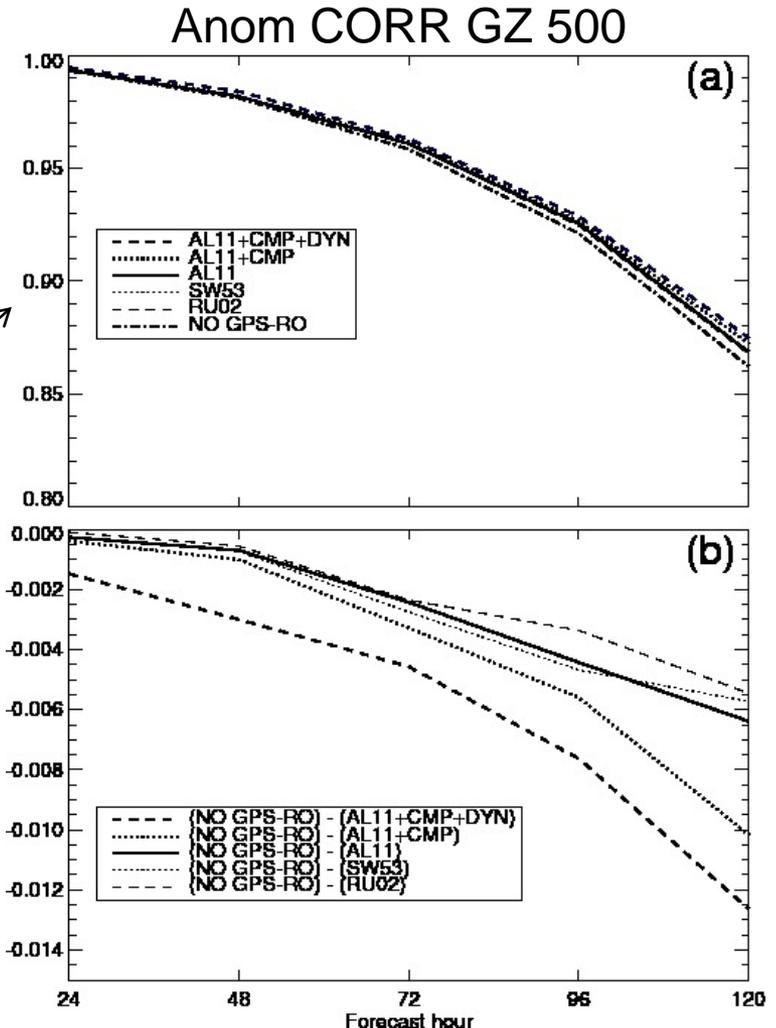
Higher at

- low T
- high P



Impact of the physical calibration

- Same other data, same NWP
- SW53, RU02, AL11 refract
- With/without RO
- Ideal gas, non-ideal
- Dynamic/static Bcor
- Above: World Anom Corr
- Below: loss of skill if we withdraw RO
- A large fraction of impact depends on constitutive relations
 - About 2x

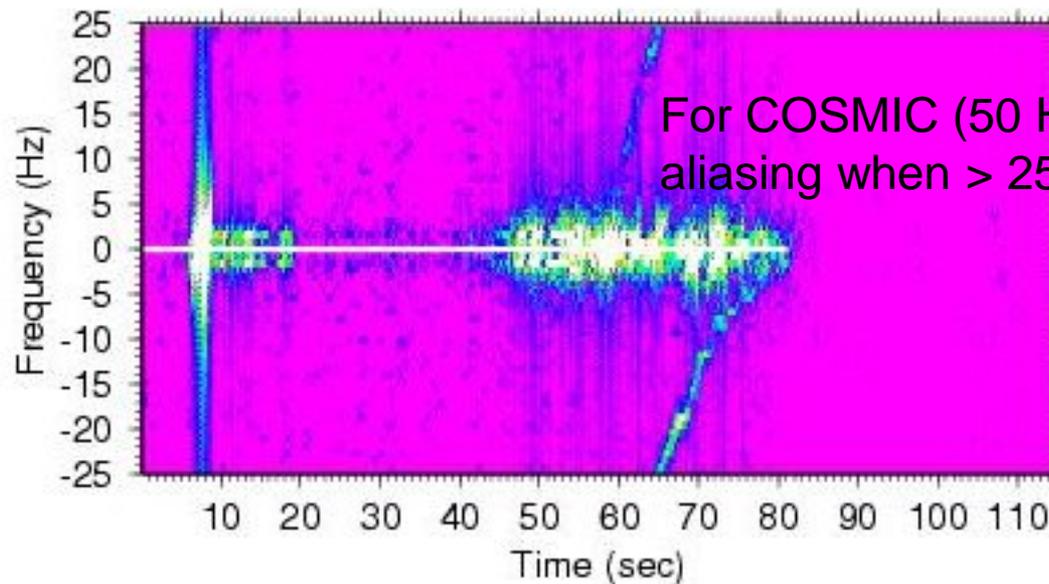
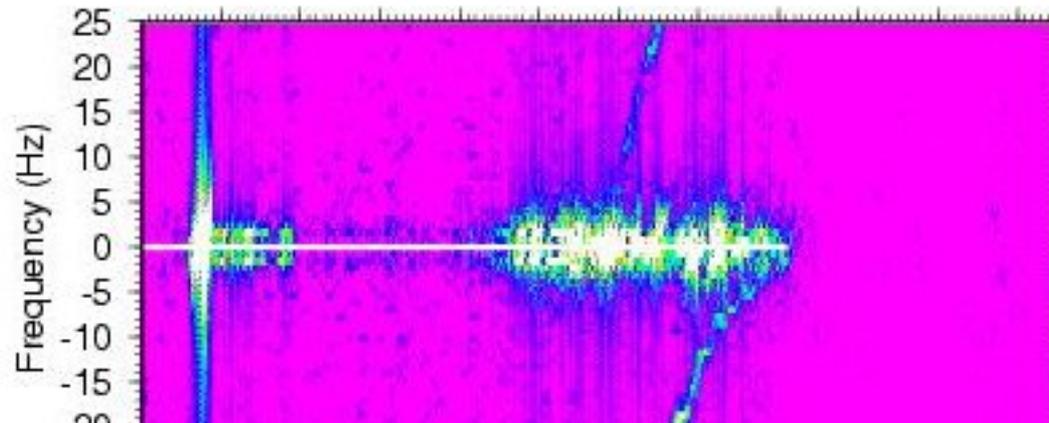


Vertical interpolation

- We have a discrete vert grid
 - Virtual T linear between grid points
 - For the hydrostatic equation
 - log N linear between grid points
 - Interpolation for refractivity operator (between grid points)
 - Derivative for the bending operator at the grid points
 - Height grid sequence assumed monotonic
 - Impact grid sequence NOT assumed monotonic
 - log α linear between grid points What about superrefraction?
 - Interpolation for bending operator (between grid points)
 - a non-monotonic: there may be jumps (superrefraction)
- Original grids P, T, q (limited by model)
 - 1st derived grids N, h, a (operator applied)
 - 2nd derived grids α (another operator applied)



Power spectrum around direct signal



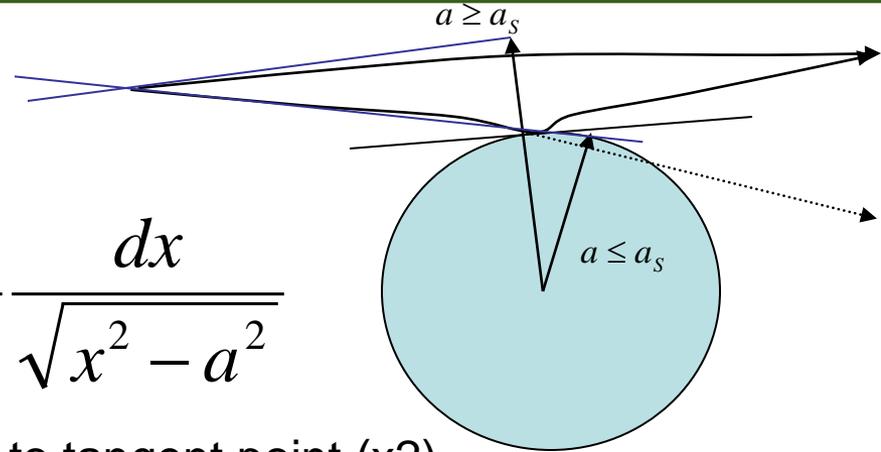
Theoretical description

$$a_s = n_s R$$

- Direct signal:

$$a \geq a_s$$

$$\alpha_D(a) = -2a \int_a^{\infty} \frac{d \ln n}{dx} \frac{dx}{\sqrt{x^2 - a^2}}$$



Refraction over the curved path, up to tangent point (x2)

- Reflected signal:

$$a \leq a_s$$

$$\alpha_R(a) = -2a \int_{a_s}^{\infty} \frac{d \ln n}{dx} \frac{dx}{\sqrt{x^2 - a^2}} - 2 \arccos\left(\frac{a}{a_s}\right)$$

Not reaching tangent point

2xElevation angle

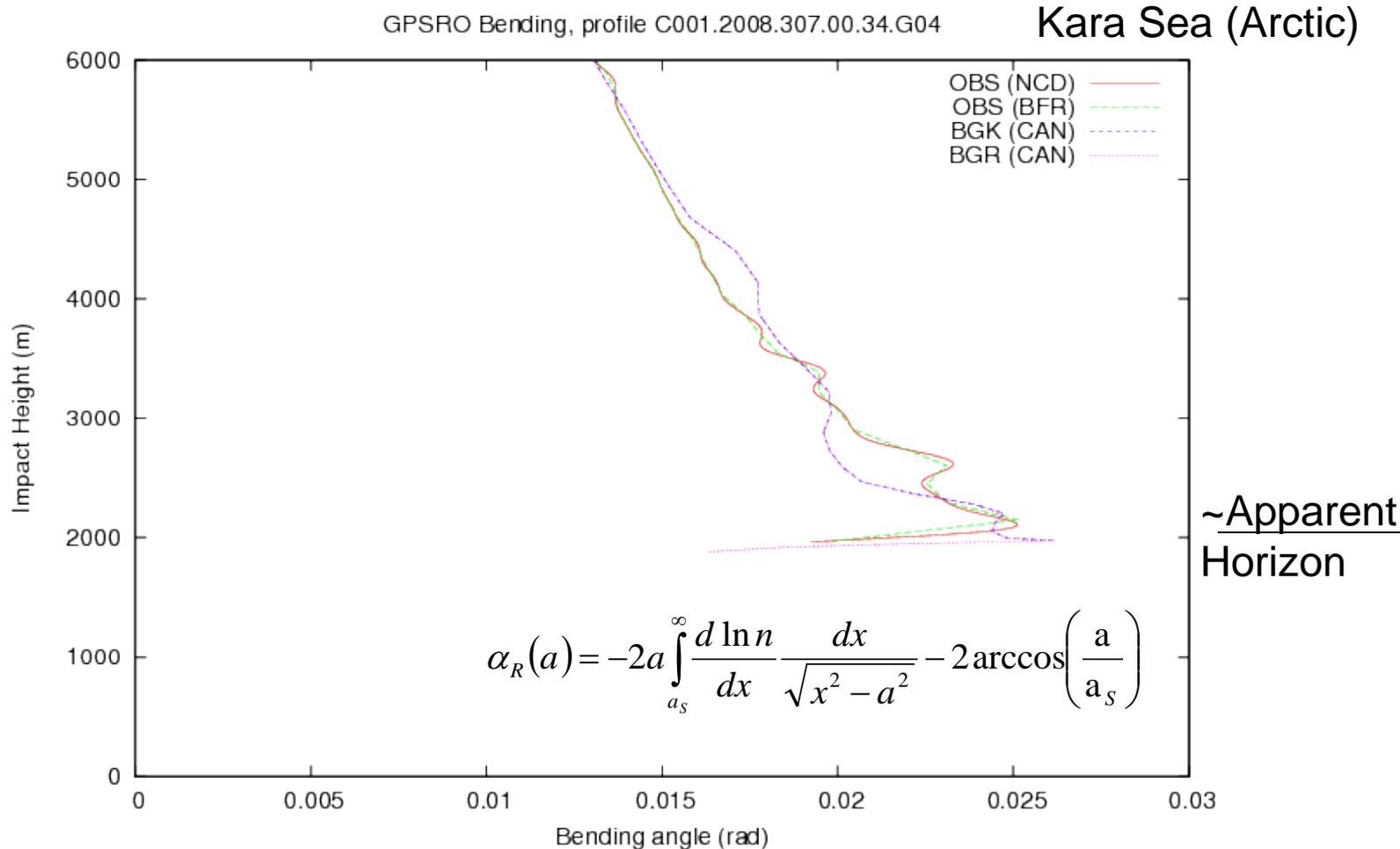
Nearly always downwards (>0)

Upwards (<0)

Impact parameter that is tangent at surface



Bending with reflection operator

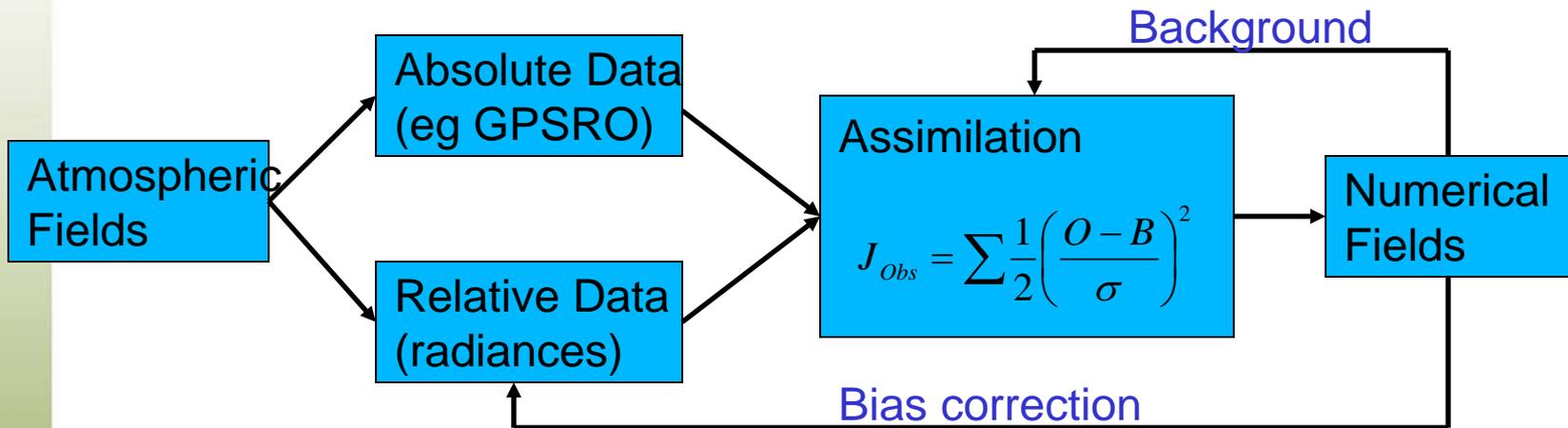


Bending operator can handle both refraction & surface reflection

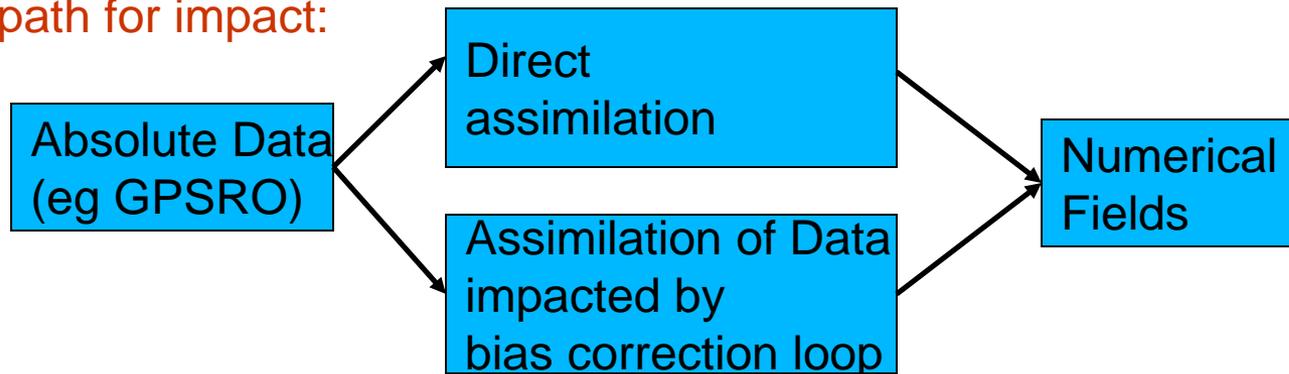
- However:
 - Standard wave optics procedures disentangle small diffraction.
 - Small multipath
 - Do they disentangle reflections?
 - Large multipath (**still entangled after backpropagation**)
- **Concern: Can upstream Doppler-to-bending processing handle true multipath?**



Information flow from data

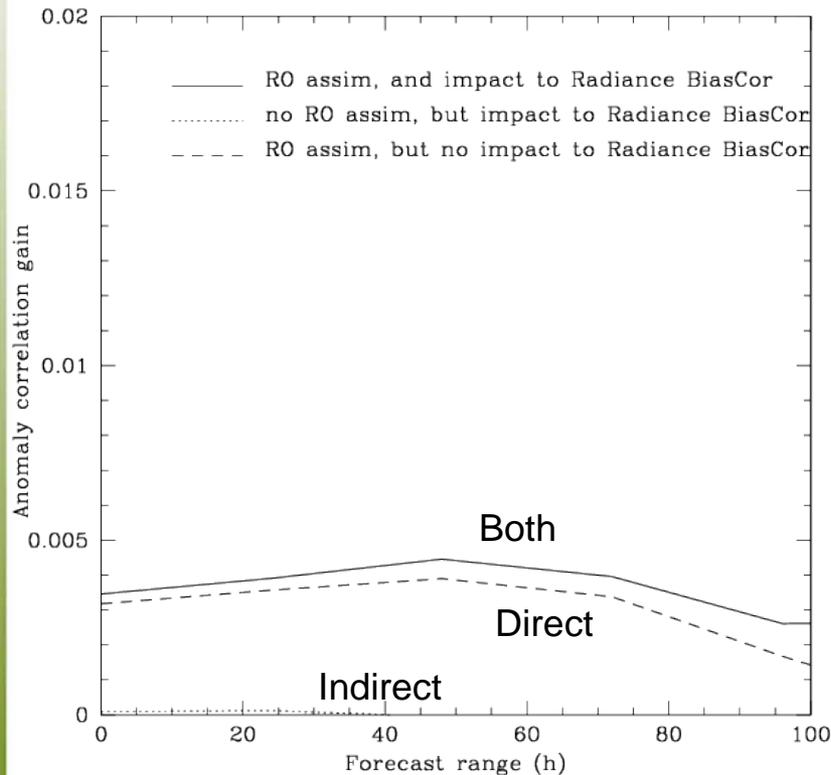


Double path for impact:

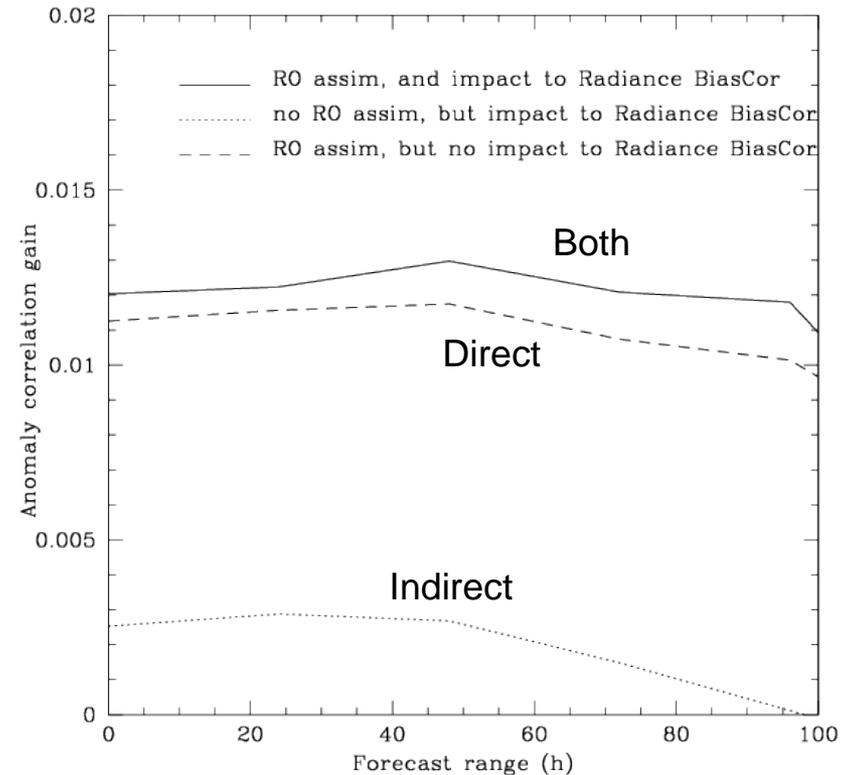


Direct and indirect impact Temp 100hPa

AC Gain, Northern Extratropics



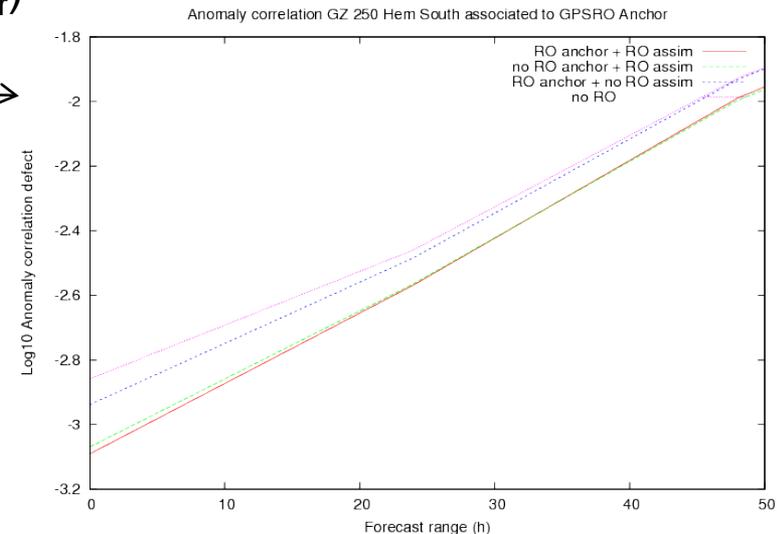
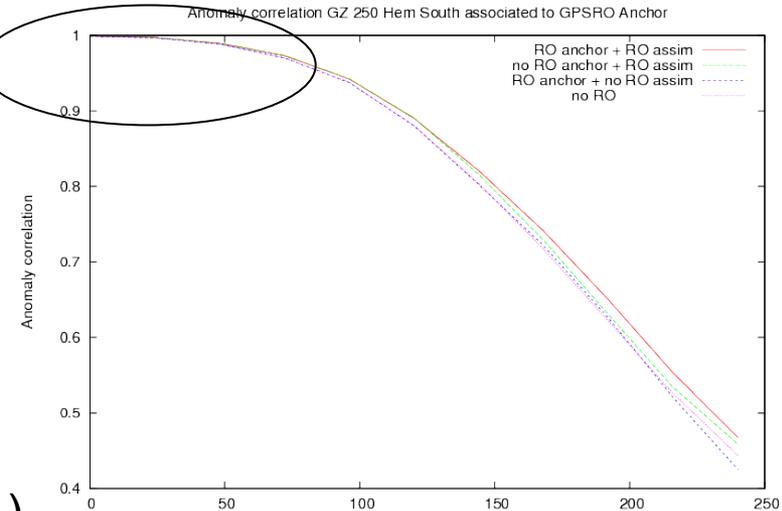
AC Gain, Southern Extratropics



GPSRO as anchor: Predictive gain

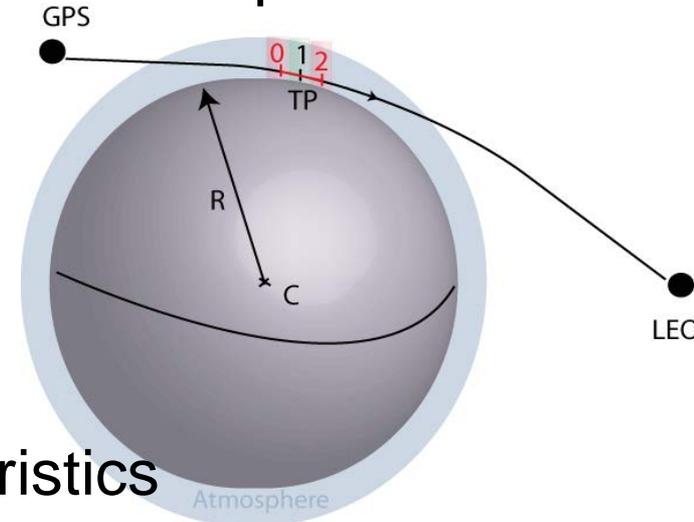
- Bias corr subsystem
 - Coefficients estimated upon "trustable" data (RS, surface, aircraft, RO)
- 4 Runs (approx what will oper this summer)
 - Full system
 - RO withdrawn from trustable subset, but kept in analysis
 - RO kept in trustable subset, withdrawn from analysis
 - RO denied

$$\log_{10}(1-A_{\text{cor}})$$

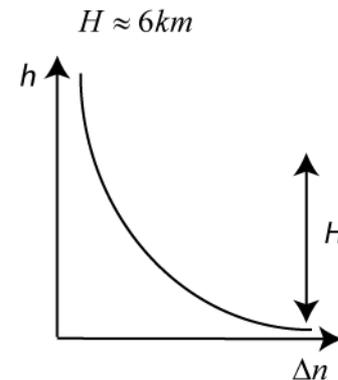
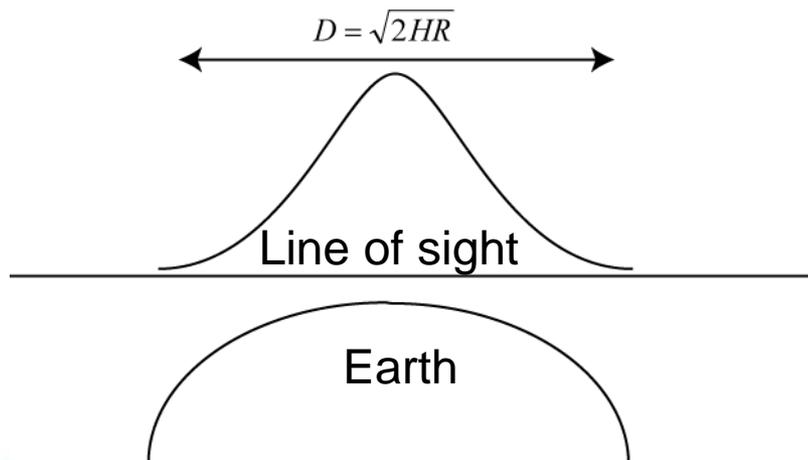


Our approach

- How atmospheric gradients have been computed ?
 - Along the ray (1D operator)
 - Location of RO profiles (1) deduced from atmprf files: *observable*
 - Atmospheric profiles location (0-2)

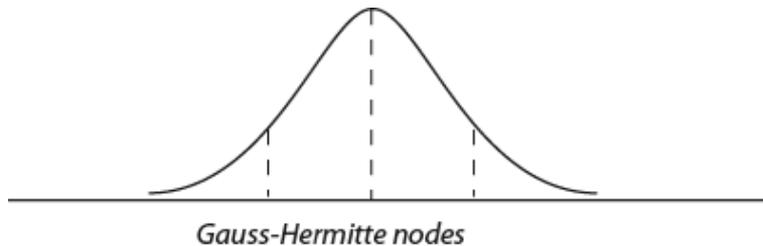


- Gradients and refractivity characteristics

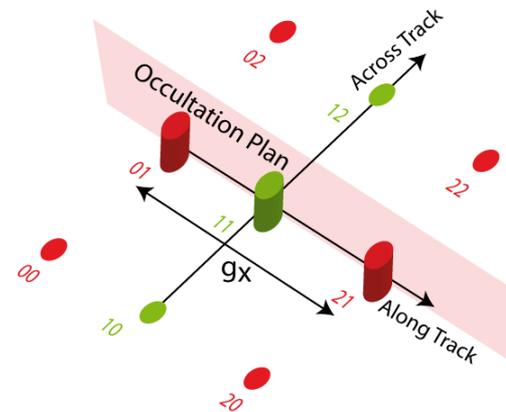


Our approach

- Characteristic size of the Gaussian region (250km)



- 3rd order Gauss-Hermite quadrature
 - Cheapest simplification of a quasi-gaussian to 3 points



Occultation plan coordinates extracted from atmPrf files

- Along track gradients are then computed with the background refractivity field from Environment Canada model



Approach for horizontal gradients

Provider-retrieved bending vs impact **assume** no gradient.

We **do** have a background value.

Dependence depends only on generic satellite geometry (simple)

Can be forward modeled from

— 1D operator results (a_0, α_0)

and

— background value of $g=dN/dx$ along line of sight

- $a = a_0 + \frac{da}{dg} g$

- $\alpha = \alpha_0 + \frac{d\alpha}{dg} g$



Critical perspective I

- Physical choices are user-side recommendations
 - Equation of state
 - Refractivity
 - Gravity acceleration
 - Careful geometry
- Anchoring properties are “nice to know” and support GPSRO as a technology within the Global Earth Obs System...
- Recommendations to providers as user?
 - Do offer **provider error estimates**
 - **All of α , a , N , h** have errors (not only α , N)
 - To consider: Can hard multipath be handled? Should?



Critical perspective II

- At Env Canada we still assimilate Refractivity
 - Not fashionable, but still peaks performance for us (because of adaptive error? Limits to the representativity of vert gradient?)
 - Not assimilated as individual data, but as **profiles**
- Refractivity data should be understood as increments
 - **Not absolute refractivity** (we do not have absolute N)
 - Provider-side Abel integral more accurate than user-side's
 - **Valid** product **if** not misused
- Low atmosphere dominated by small scale structure
 - better use bending
 - Injects info at higher vertical wavenumber
 - Can handle reflection data



Critical perspective III (Our plan)

- Keep profile-oriented assimilation (not datum-oriented)
- Can we use a mixed approach?
 - Both bending and refractivity vectors used (not double assim!)
 - Info injection in upper atmosphere at low wavenumber
 - through thick layers (N increments, not N!)
 - Info injection in low troposphere at high wavenumber
 - through thin layers (Bending, reflection)
- Is hard multipath a problem?
 - Multipath that does not resolve with backpropagation/similar.
- Horiz Gradients:
 - **Large scale** (smooth) gradients tractable (Boniface et al, IROWG-2)
 - We do plan to include these
 - With small structure: technologically **impractical for ops** in near future



Thank you

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