

First lessons learnt from Metop

Peter Schlüssel

With thanks to Jörg Ackermann, Arlindo Arriaga, Thomas August, Hans Bonekamp, Xavier Calbet, Lars Fiedler, Tim Hultberg, Dieter Klaes, Xu Liu, François Montagner, Éamonn McKernan, Olusoji Oduleye, Bill Smith, Jon Taylor

EUMETSAT
Darmstadt, Germany

Initial Joint Polar System

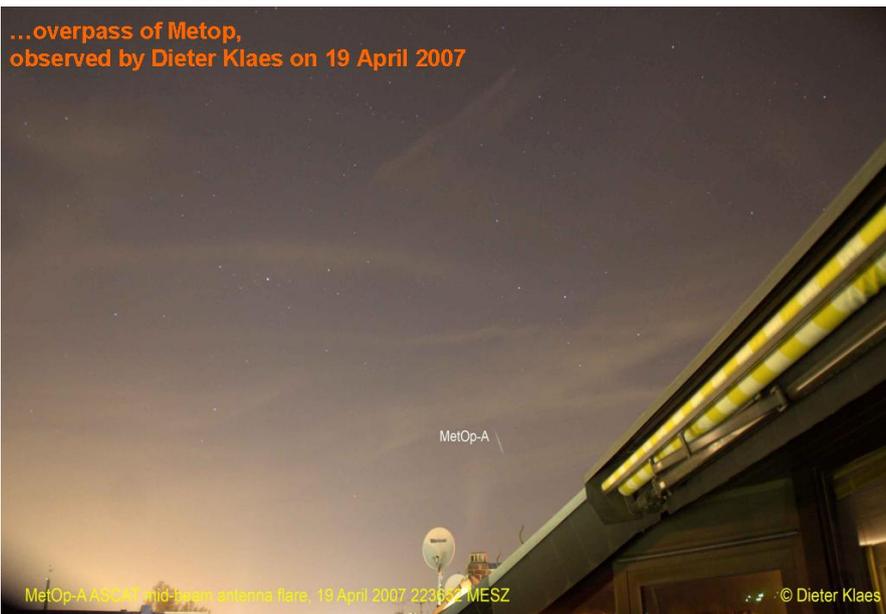
- Since 1978 NOAA is flying operational polar orbiting weather satellites carrying multi-spectral sounders and imagers
- Under a NOAA-EUMETSAT cooperation agreement, signed in November 1998, Europe agreed to share the burden of the meteorological polar service with the USA
- Integration and coordination of the NOAA Polar Orbiting Environmental Satellite (POES) and the EUMETSAT Polar System (EPS) Programmes:
 - Afternoon & early morning orbits covered by the USA (POES & DMSP Satellites)
 - Mid-morning orbit covered by Europe (Metop Satellites)
 - Exchange of instruments and data, coordinated development and operations
- Joint effort in a partnership of ESA, NOAA, CNES, and EUMETSAT

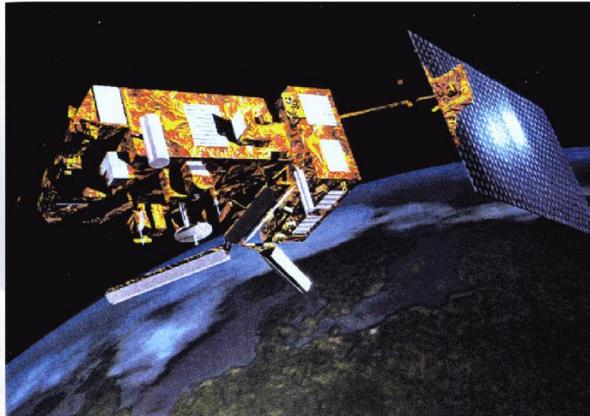
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Height: 6.3 m
Transverse Section:
3.4 m x 3.4 m
(Launch Configuration)

Solar Panel: 11.3 m

Power: 2210 W
(End of Life, Orbit Average)

Lifetime: 5 Years

12 Instruments

Launch Mass: 4200 kg

Data Flow: 3500 kbps

The Metop Satellite

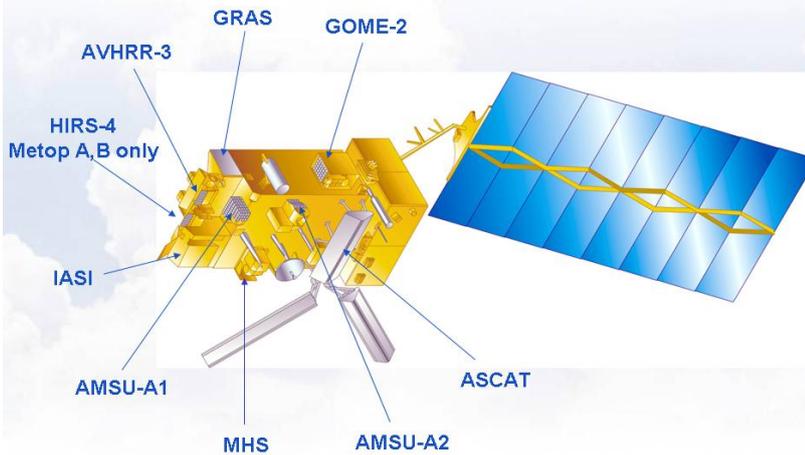
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Metop: Satellite and Met-Instruments



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Metop during integration of instruments



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From launch to operational use (1/2)

- Launch on 19 October 2006 from Cosmodrome in Baikonur
 - Start and transfer to final orbit by ESA/ESOC
 - Handover to EUMETSAT: 22 October 2006
- Successive switch-on of instruments and distribution of data
 - SARR, SARP instrument switch on: 24 October 2006
 - AMSU-A1/A2 instrument switch-on: 24 October 2006
 - First global AMSU-A data distributed in NRT: 31 October 2006
 - IASI instrument switch-on and start of outgassing: 24 October 2006
 - AVHRR instrument switch-on and outgassing: 25 October 2006
 - First generation of AVHRR L1 products (VIS, NIR): 25 October 2006
 - HIRS instrument switch-on and outgassing: 26 October 2006
 - A-DCS instrument switch-on: 26 October 2006
 - GRAS instrument switch-on: 27 October 2006
 - ASCAT instrument switch-on and first product generated: 27 October 2006

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From launch to operational use (2/3)

- Successive switch-on of instruments and distribution of data (cont.)
 - GOME-2 instrument switch-on: 27 October 2006
 - GOME-2 first spectra: 30 October 2006
 - MHS instrument switch-on and first data: 31 October 2006
 - MHS first L1 products generated: 1 November 2006
 - SEM instrument switch-on: 9 November 2006
 - ASCAT in measurement mode: 20 November 2006
 - A-DCS instrument switch-on: 20 November 2006
 - AVHRR, HIRS, GOME-2 in measurement mode:
 - LRPT switch-on: 15 January 2007
 - AHRPT switch-on: 23 January 2007
 - LRPT switch-off permanently (RFI with HIRS): 26 January 2006
- 4 November 2006: Two anomalies abruptly stopped the sequence of success
 - Sudden failure within the Low Resolution Picture Transmitter (LRPT)
 - Sudden automatic switch-off of the complete Metop-A Payload Module, with all instruments.

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From launch to operational use (3/3)

- Progressive dissemination of data to users
 - Monitoring by NWP centres (ECMWF and Met Office) provides valuable information on data quality and anomalies
 - First global AMSU-A data distributed in NRT: 31 October 2006
 - Met Office starts assimilation of AMSU-A data on 22 January 2007
 - ECMWF starts assimilation of IASI data on 12 May 2007
 - Cooperation with OSI SAF leads to successful calibration of ASCAT despite failure of calibration transponders
- Completion of Metop-A Satellite In-Orbit Verification (SIOV): 30 March 2007
- Hand-over to operations: 21 May 2007

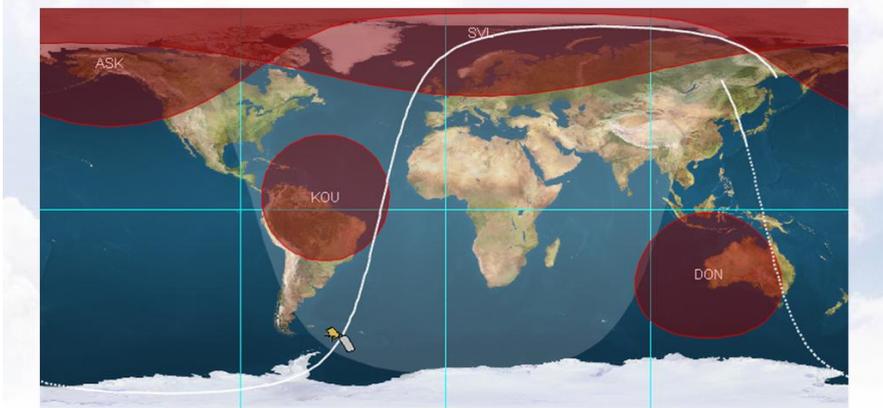
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Metop-A control during SIOV



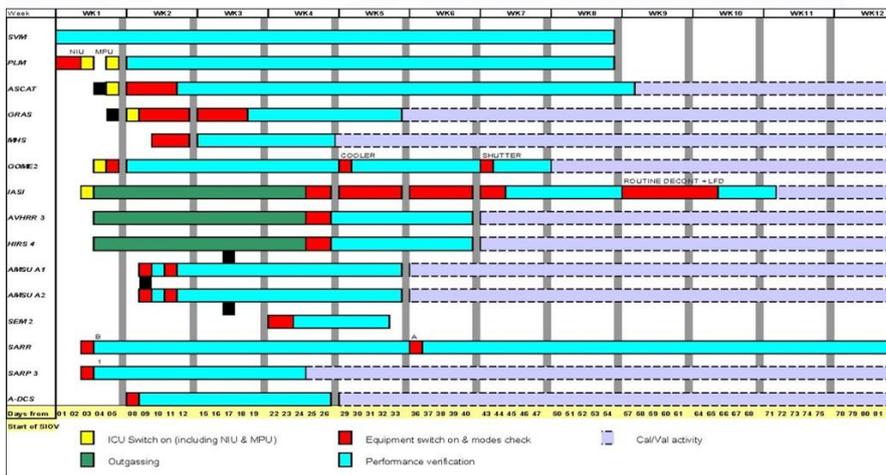
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Metop-A Satellite In-Orbit Verification



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Validation

- Validation of processors and products
 - Configuration of Product Processing Facilities
 - First rough validation including bias corrections in Level 2 processors using short-range forecasts
 - Refinement with data from dedicated validation campaigns
- Campaigns:
 - ASCAT transponder-campaign Turkey, November 2007
 - CNES/CNRS IASI-Balloon: Kiruna, February 2007
 - Met Office FAAM: Western North Sea, March 2007
 - IfM/Polarstern: Atlantic Ocean, April/May 2007
 - Met Office/NASA FAAM and WB-57: Gulf of Mexico and Oklahoma ARM-Site, April/May 2007
 - DWD: Assmann-Observatory Lindenberg, June-August 2007
 - FMI: Observatory Sodankylä, June-August 2007
 - CNES/CNRS IASI-Balloon: Kiruna, September 2007
 - .
 - .

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Partnership (1/2)

- The EPS programme was set up in partnership with
 - ESA (for the development of the Metop space Segment)
 - NOAA (provision of US instruments and operational cross support)
 - CNES-IASI (Development of the IASI instrument, level 1 processor and Technical Expertise Centre)
 - CNES-ARGOS (A-DCS payload and operations)
- The Space Segment development was managed by the Single Space Segment Team (SSST) located at ESTEC, Noordwijk
- The Metop-A satellite was developed by a European consortium led by Astrium as the prime contractor under a joint ESA-EUMETSAT contract
- The Launch service was provided by Starsem using a Soyuz 2.1 a with an ST fairing launcher from the Baikonur Cosmodrome, under EUMETSAT Contract

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Partnership (2/2)

- The Launch and Early Operations Phase (LEOP) was conducted by ESOC, Darmstadt, under EUMETSAT contract
- The Core Ground Segment was developed by Thales Alenia Space under EUMETSAT contract
- The Satellite SIOV activities were conducted by a joint team led by the SSST, EUMETSAT being responsible for the operations, and with contributions from all other partner organisations and industrial teams from the space segment and instrument manufacturers
- Last but not least: EUMETSAT users provide valuable feedback
 - Throughout the programme development on instrument characteristics, system configurations, product processing and product formats
 - Post-launch via data monitoring and data usage

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Satellite Application Facilities (SAF)

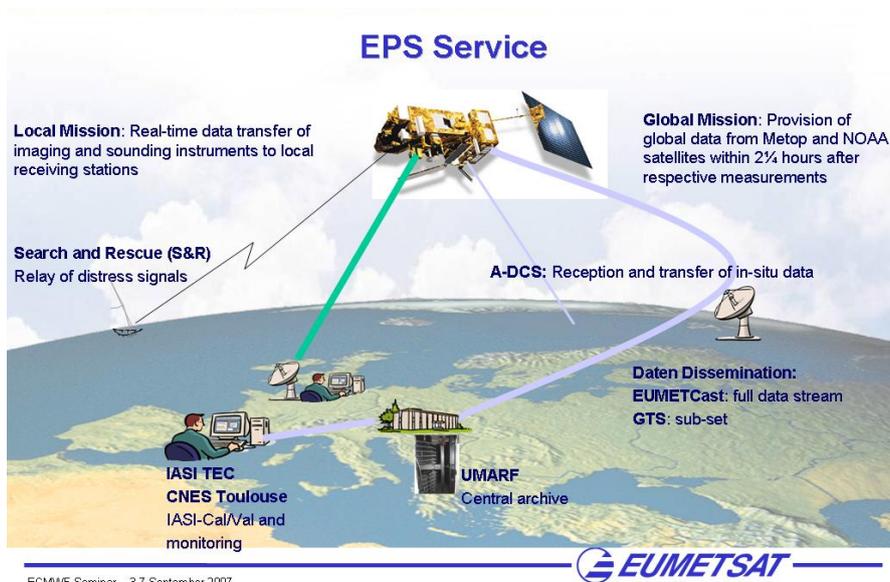


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Data transfer and distribution

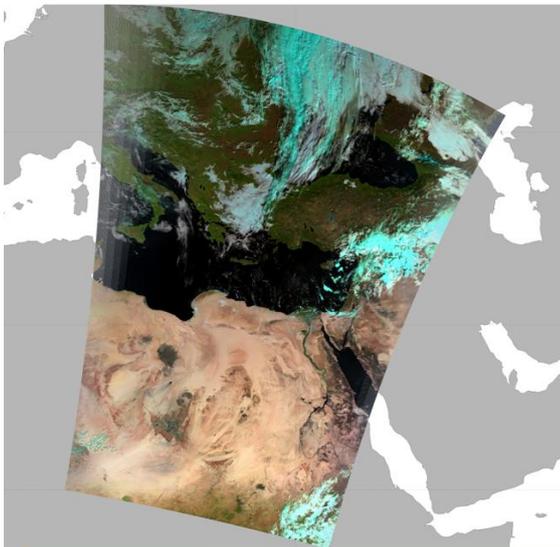
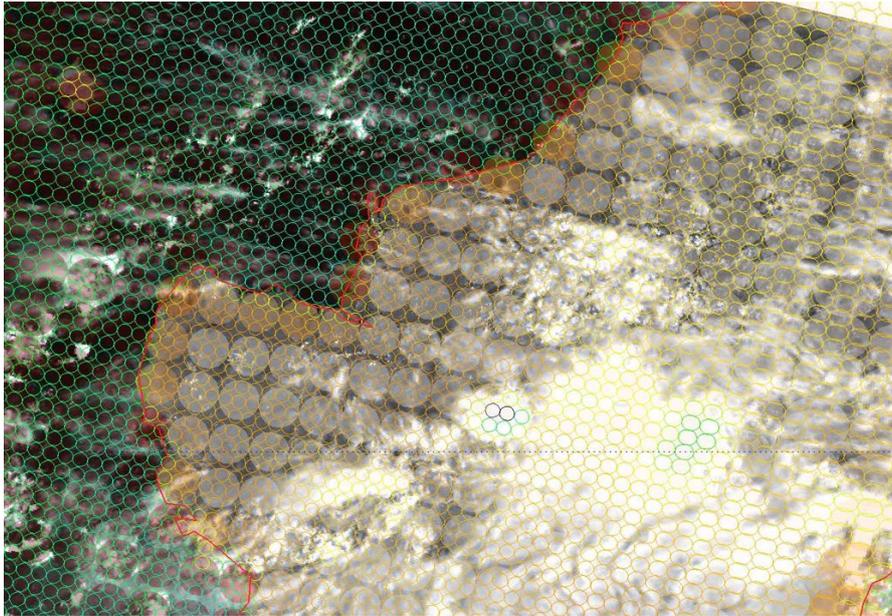
- From satellite to surface:
 - Data of one orbit is stored on board the satellite
 - Transfer to surface via X-band reception station on Svalbard after completion of each orbit
 - Transfer from Svalbard to Darmstadt via fibre link
 - Local users can directly read out the instrument data while the satellite is above their horizon
- Data processing in EPS Core Ground Segment at EUMETSAT HQ
 - Generation of Level-1-Products: decoding, calibration, navigation, apodisation, mapping/merging of data from different instruments
 - Generation of ATOVS and IASI Level-2-Products: atmospheric and surface meteorological parameters
- Distribution to users:
 - Level 1: within 2¼ h after measurement, Level 2: within 3 h after measurement
 - Transfer via EUMETCast (BUFR code)
 - Transfer of subset via GTS (BUFR code)
 - All data, inclusive generated products are archived in the UMARF: Unified Archival and Retrieval Facility, and accessible 7 hours after the measurement

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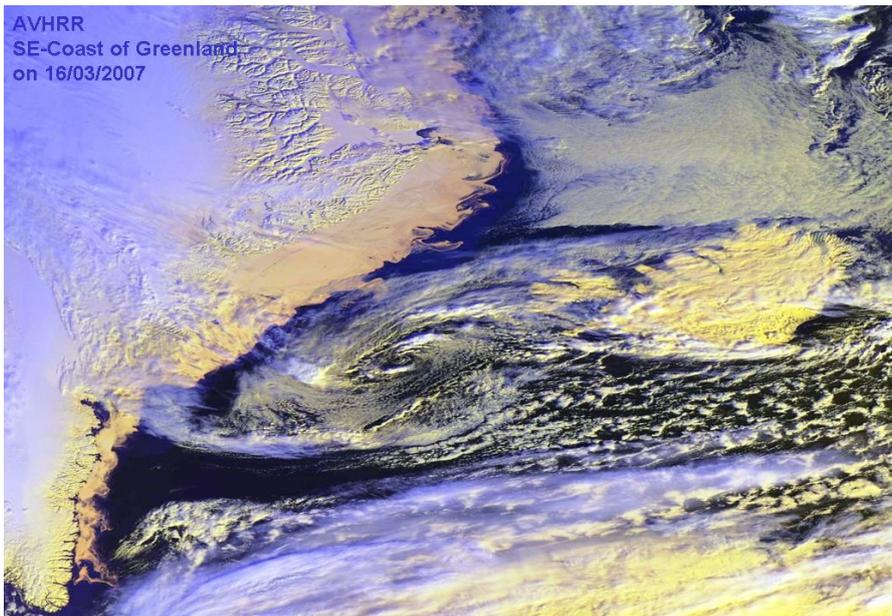
First AVHRR data
on 25/10/2006



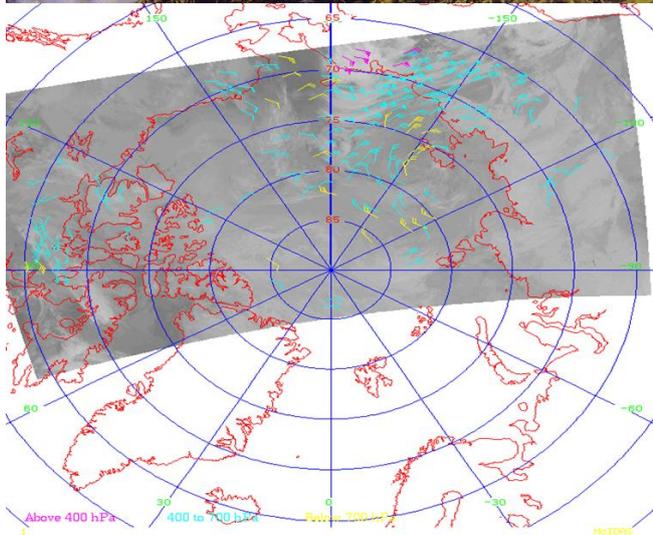
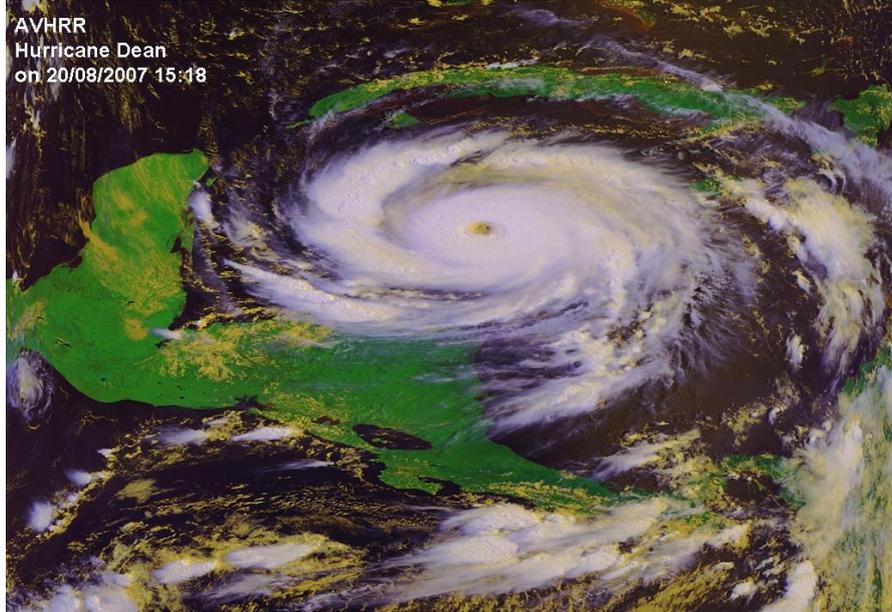
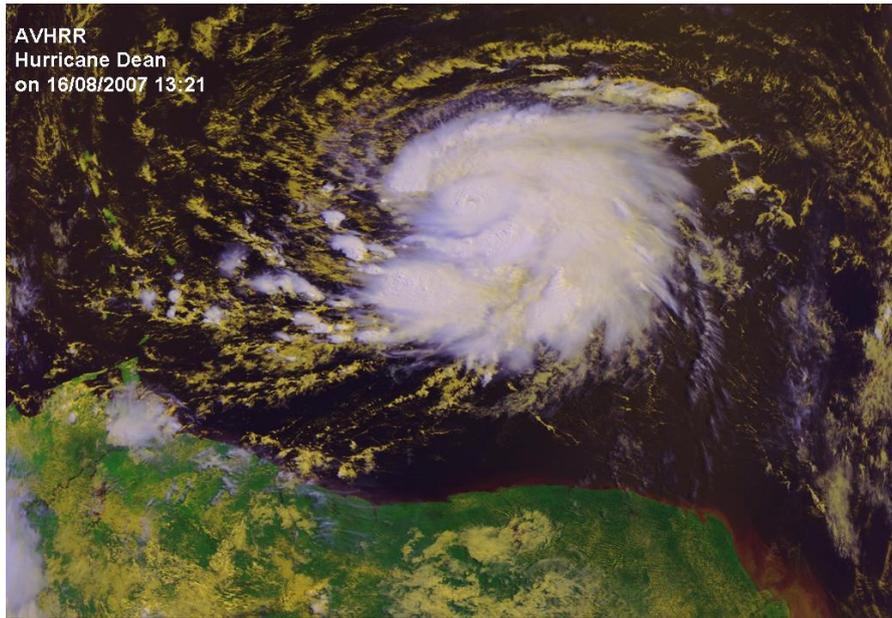
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AVHRR
SE-Coast of Greenland
on 16/03/2007

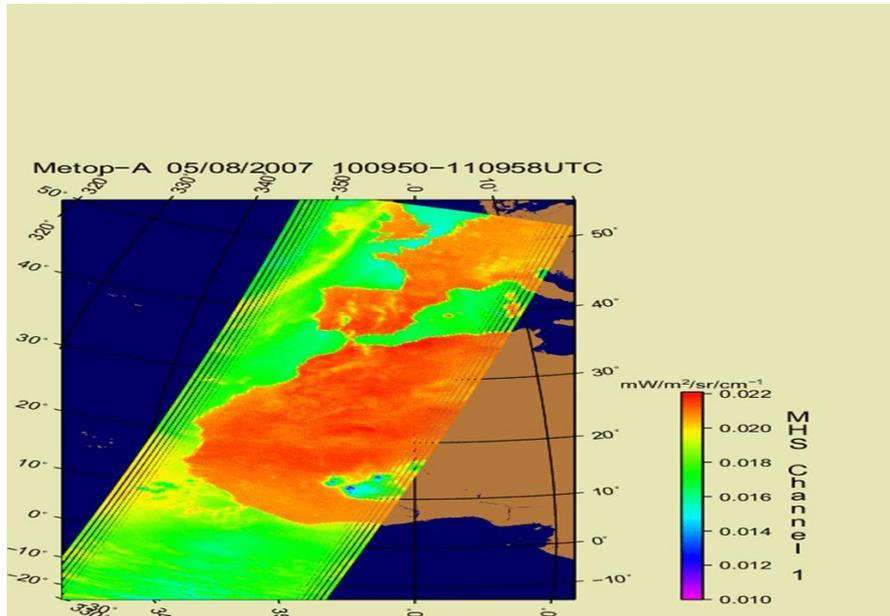
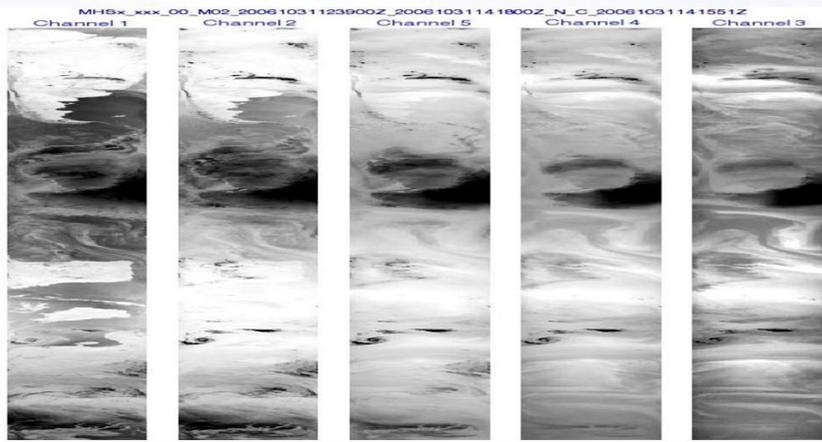


AVHRR:
Wind vectors in polar regions

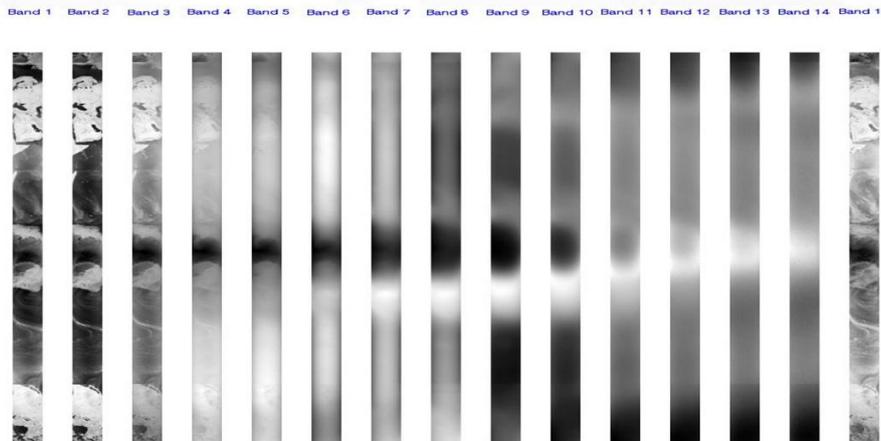
CIMSS/Univ. Wisconsin

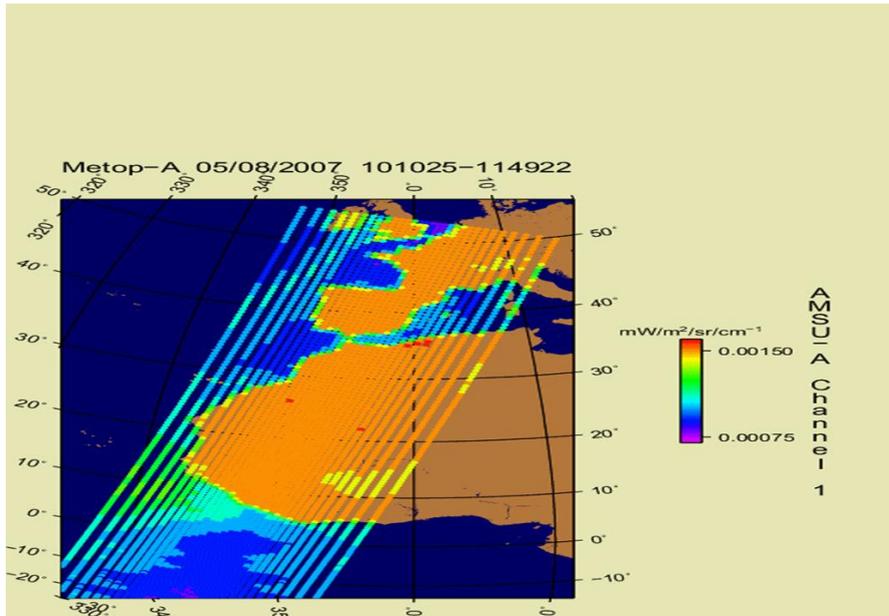


MHS



AMSU-A

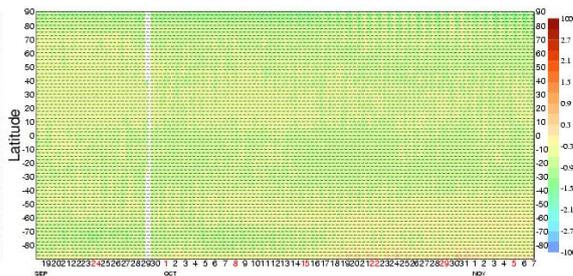
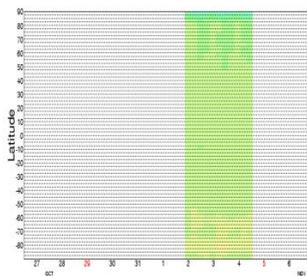




ECMWF monitoring the data from the beginning

STATISTICS FOR RADIANCES FROM METOP-A / AMSU-A
 ZONAL MEAN FIRST GUESS DEPARTURE (OBS-FG) [K] (CLEAR)
 CHANNEL = 10
 EXP = 0001
 Min: -1.9787 Max: -0.227095 Mean: -0.780688

STATISTICS FOR RADIANCES FROM NOAA-18 / AMSU-A
 ZONAL MEAN FIRST GUESS DEPARTURE (OBS-FG) [K] (CLEAR)
 CHANNEL = 10
 EXP = 0001
 Min: -1.607 Max: 0.465248 Mean: -0.607009



**Feedback from Met Office
 AMSU-A noise figures (NEΔT in K)**

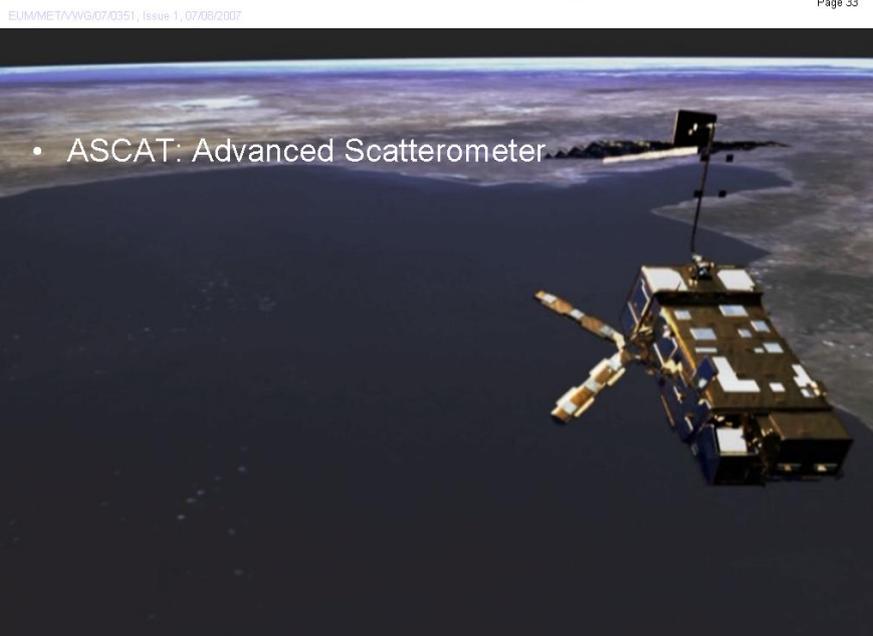
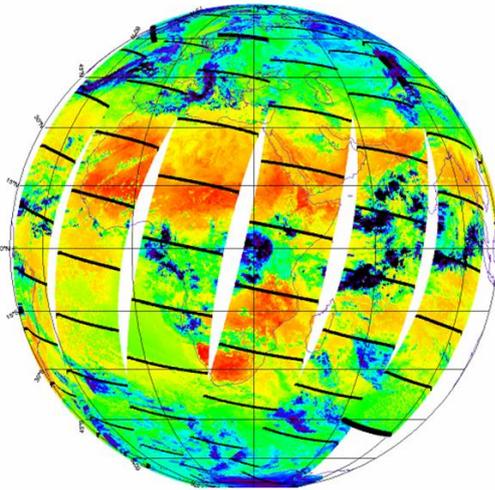
Channel	Spec	Met Office estimate	NOAA-18	Channel	Spec	Met Office estimate	NOAA-18
1	0.3	0.19	0.20	9	0.25	0.18	0.17
2	0.3	0.19	0.18	10	0.4	0.24	0.20
3	0.4	0.28	0.22	11	0.4	0.29	0.23
4	0.25	0.15	0.16	12	0.6	0.37	0.29
5	0.25	0.15	0.18	13	0.8	0.52	0.40
6	0.25	0.12	0.15	14	1.2	0.92	0.63
7	0.25	0.13	0.16	15	0.5	0.10	0.14
8	0.25	0.19	0.20				

Feedback from Met Office MHS noise figures (NE Δ T in K)

Channel	Spec	EUMETSAT estimate	Met Office estimate	NOAA-18 EUM/NOAA	AMSU-B EUM/NOAA
1	1.0	0.19	0.20	0.21/0.32	0.41/0.40
2	1.0	0.39	0.37	0.34/0.53	0.80/0.80
3	1.0	0.52	0.50	0.54/0.50	0.82/0.80
4	1.0	0.40	0.41	0.40/0.41	0.75/0.75
5	1.0	0.36	0.34	0.55/0.55	0.80/0.80

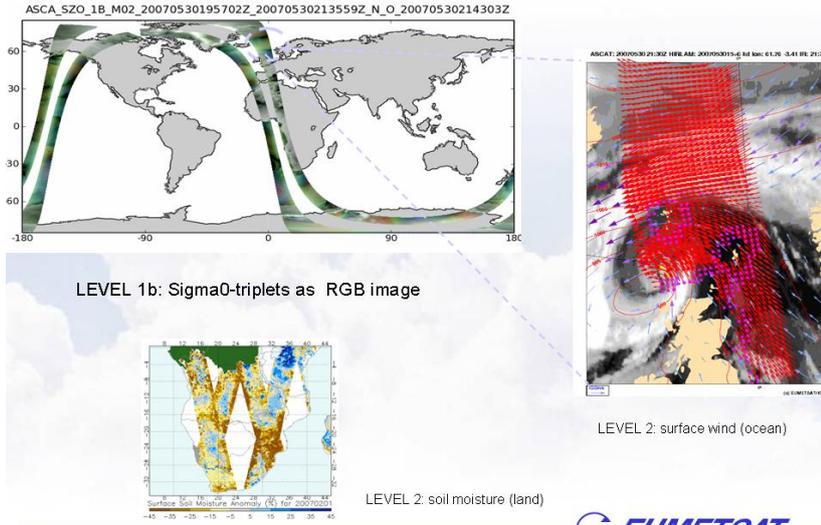
HIRS Channel 8

21 November 2006



- ASCAT: Advanced Scatterometer

SCHLÜSSEL, P.: FIRST LESSONS LEARNT FROM METOP



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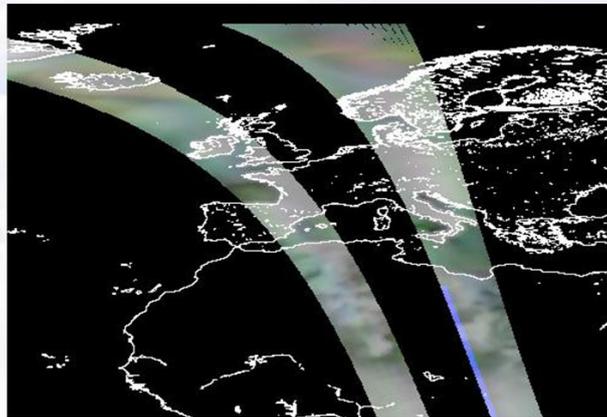


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ASCAT

Normalised backscatter coefficients (σ_0)



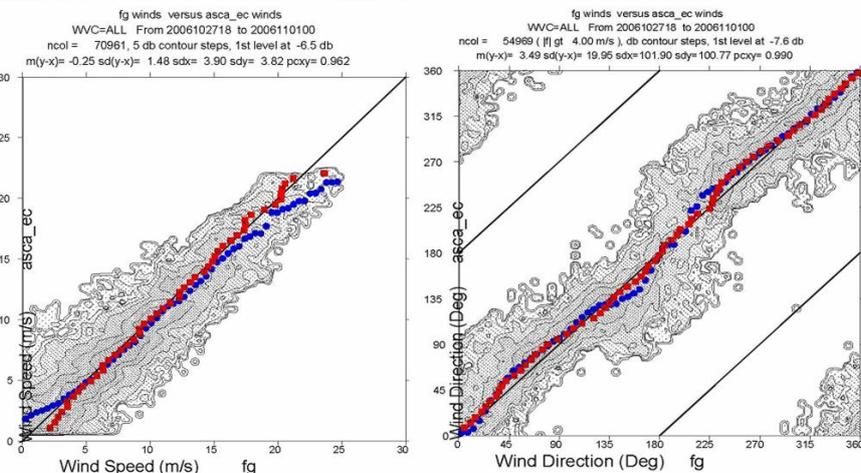
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ASCAT: first comparisons by ECMWF



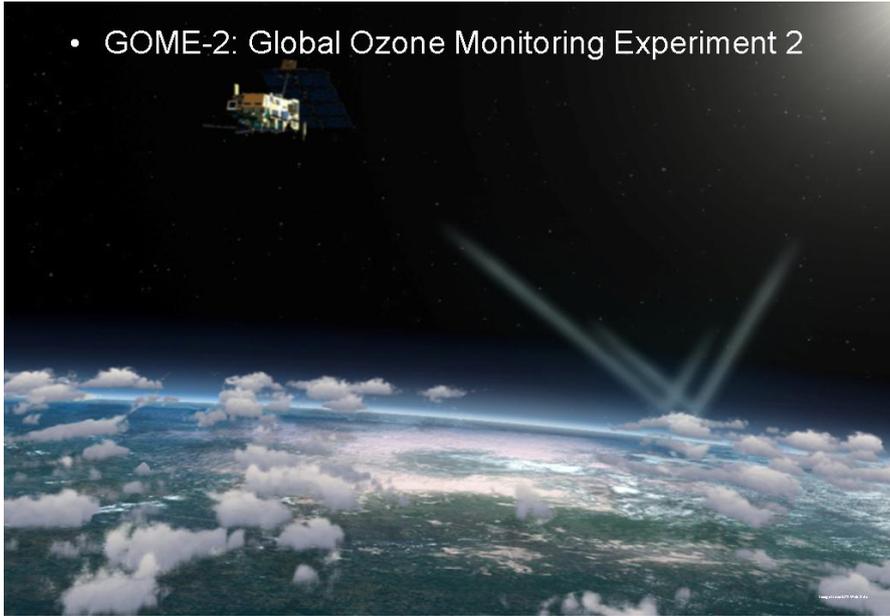
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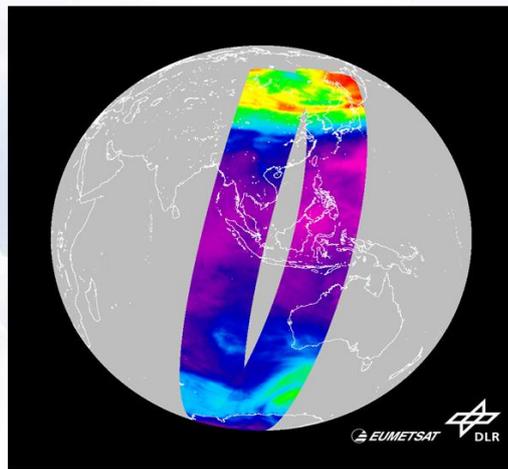
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- GOME-2: Global Ozone Monitoring Experiment 2



First GOME-2 ozone columnar contents



Ozone SAF Project

Loyola, 2007



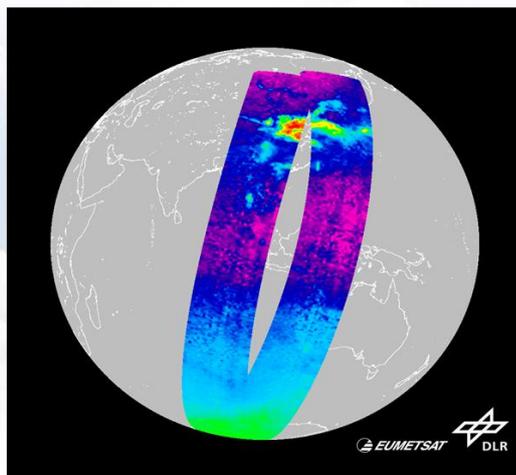
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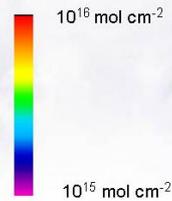
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First GOME-2 NO₂ columnar contents



Ozone SAF Project

Loyola, 2007

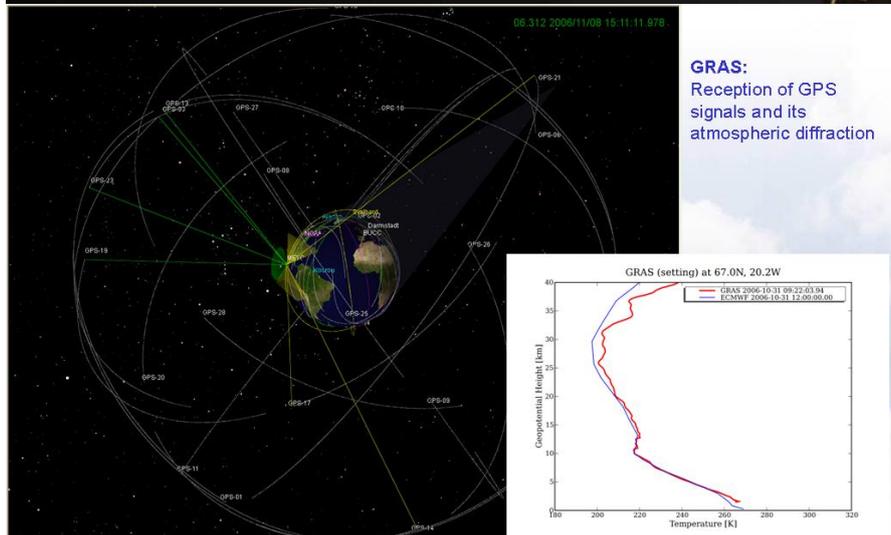
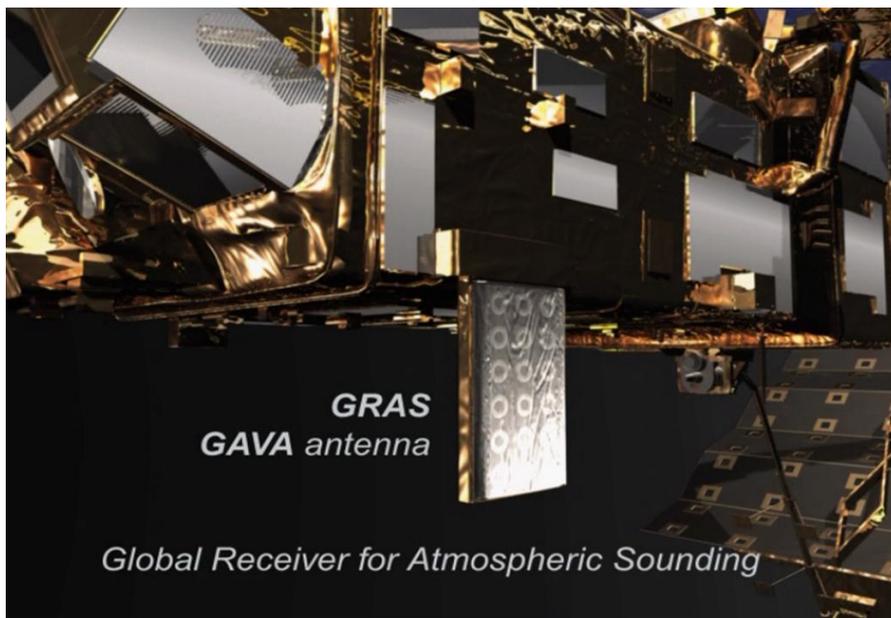


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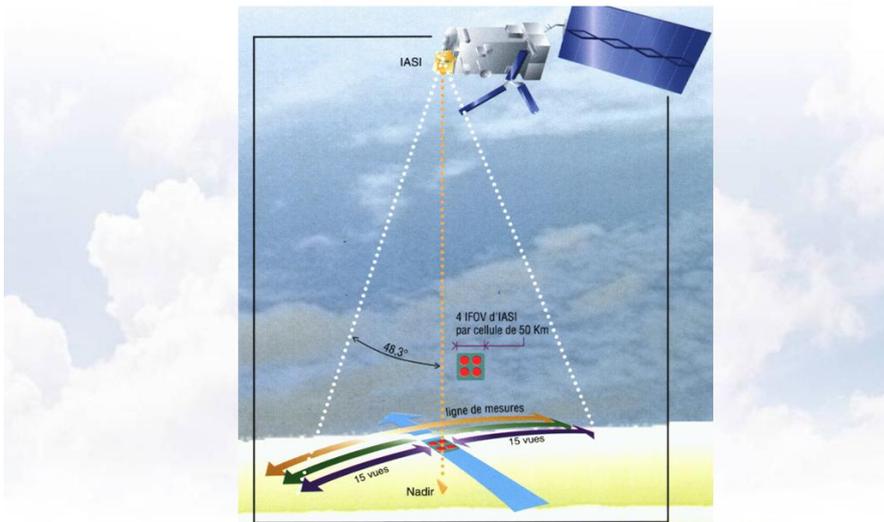
EUMETSAT

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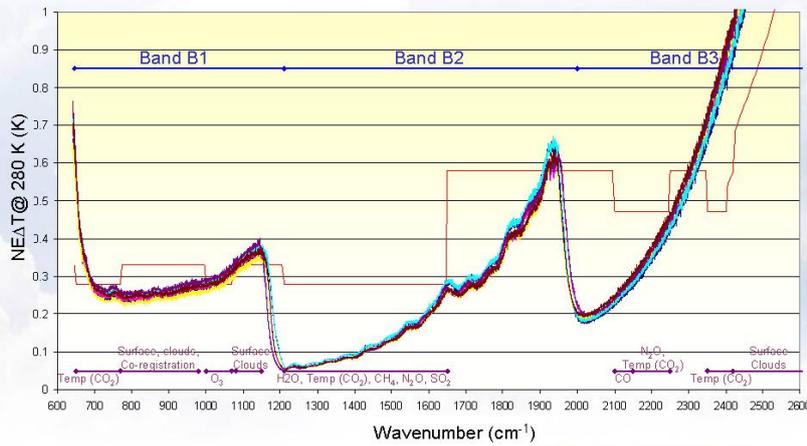


Infrared Atmospheric Sounding Interferometer (IASI)

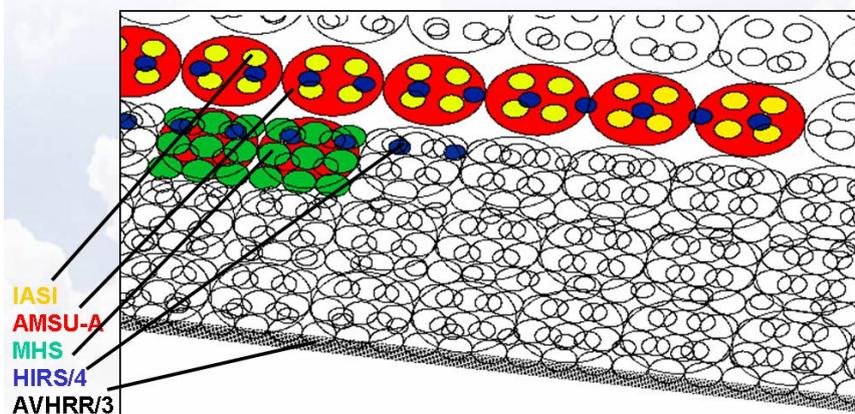
- Michelson-Interferometer 8461 spectral samples
- IFOV diameter 12 km (nadir)
- Scan interval (horiz.) 25 km (nadir)
- Swath width $\pm 48.33^\circ$ (2200 km)
- Spectral domain 645 - 2760 cm^{-1} (3.6 – 15.5 μm)
- Spectral resolution 0.5 cm^{-1}
- Radiometric resolution 0.07 - 0.7 K (bands 1, 2)
- Absolute calibration < 0.3 K
- Data rate 1.5 Mbit/s
- Internal imager 10-12 μm
- Temperature- and humidity profiles, O_3 , CO, CO_2 , CH_4 , N_2O , ...



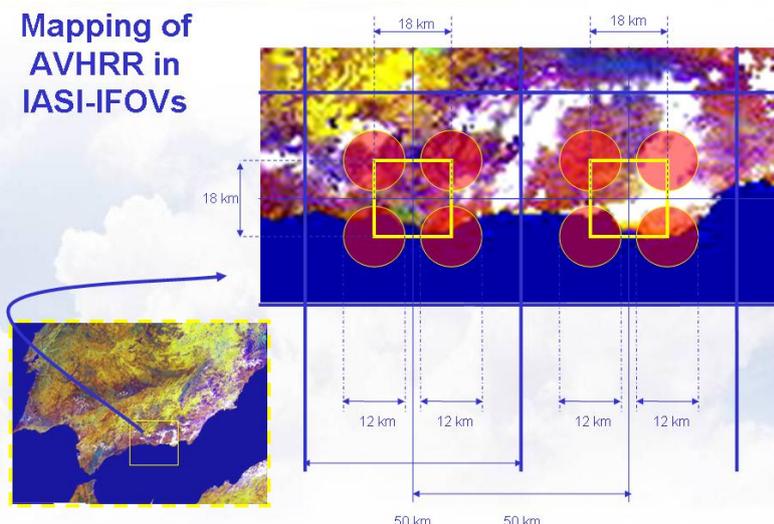
IASI FM-2: Radiometric noise



Scan patterns of the instruments



Mapping of AVHRR in IASI-FOVs



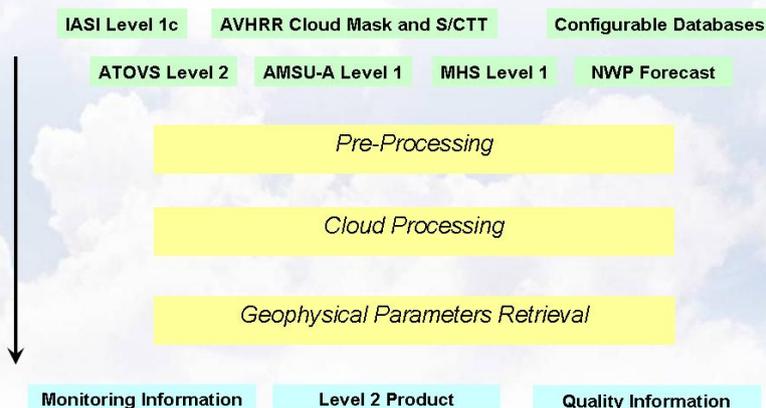
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IASI Level 2 product generation



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Properties of the Operational IASI L2 Processor (1/3)

- For a best use of IASI measurements the level 2 processing can combine IASI with concurrent measurements of AVHRR, AMSU-A, MHS, and ATOVS Level 2 products
- IASI stand-alone processing is possible if other measurements are not available, or if Product Processing Facility is explicitly configured to exclude other instruments
- NWP forecast is included to provide surface pressure as reference for the profiles to be retrieved and surface wind speed over sea for the calculation of surface emissivity
- Optionally, the NWP forecast profiles of temperature, water vapour and ozone can be used to initialise and/or constrain the retrieval

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Properties of the Operational IASI L2 Processor (2/3)

- Processing is steered by configuration settings (80 configurable auxiliary data sets), which allows for optimisation of Product Processing Facility before and during commissioning
- Online quality control supports the choice of best processing options in case of partly unavailable IASI data or corrupt side information (data from other instruments or NWP forecast)
- Besides error covariances a number of flags are generated steering through the processing and giving quality indicators; 40 flags are specified, which are part of the product

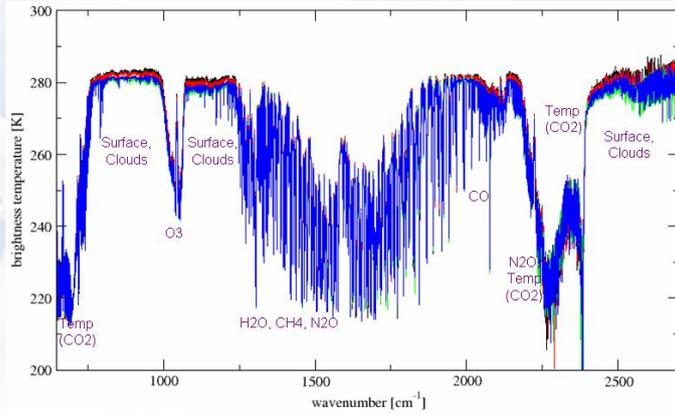
Properties of the operational IASI L2 Processor (3/3)

- All 8461 IASI spectral samples, covering the spectral region from 645 to 2760 cm^{-1} , are used in the retrieval to maximise the retrieved information
- The Product Processing Facility supports nominal and degraded instrument modes (e.g. failure of single detectors/bands)
- Bias control by radiance tuning via configuration

Cloud processing

- Cloud detection
 - AVHRR-based cloud detection using Scenes Analysis from AVHRR Level 1 processing
 - Combined IASI / ATOVS cloud detection
 - IASI stand-alone cloud detection
- Cloud parameters retrieval
 - Cloud fraction
 - Cloud top height
 - Cloud phase

First IASI spectra on 29 November 2006



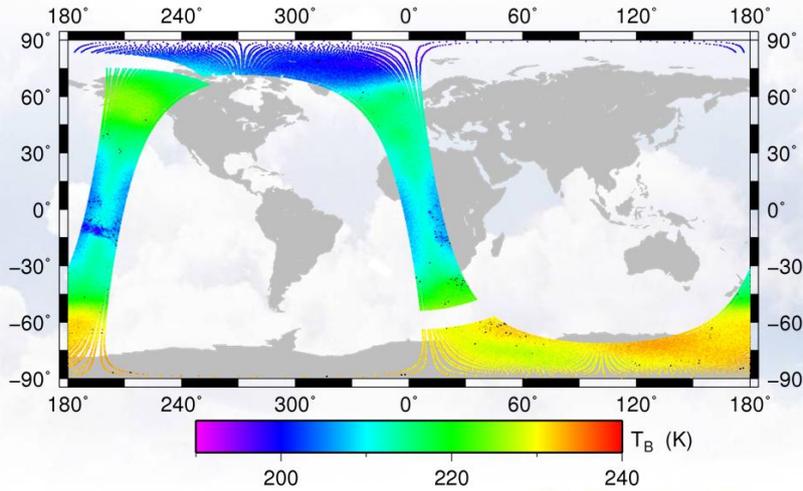
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IASI – 645 cm⁻¹



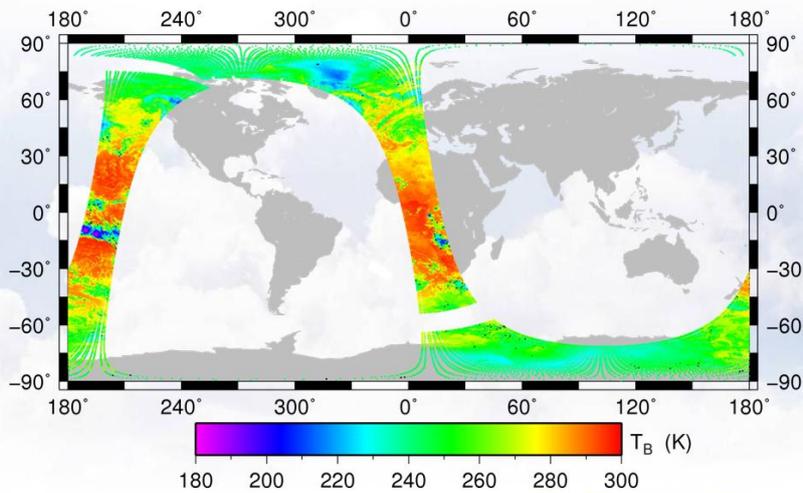
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IASI – 945 cm⁻¹

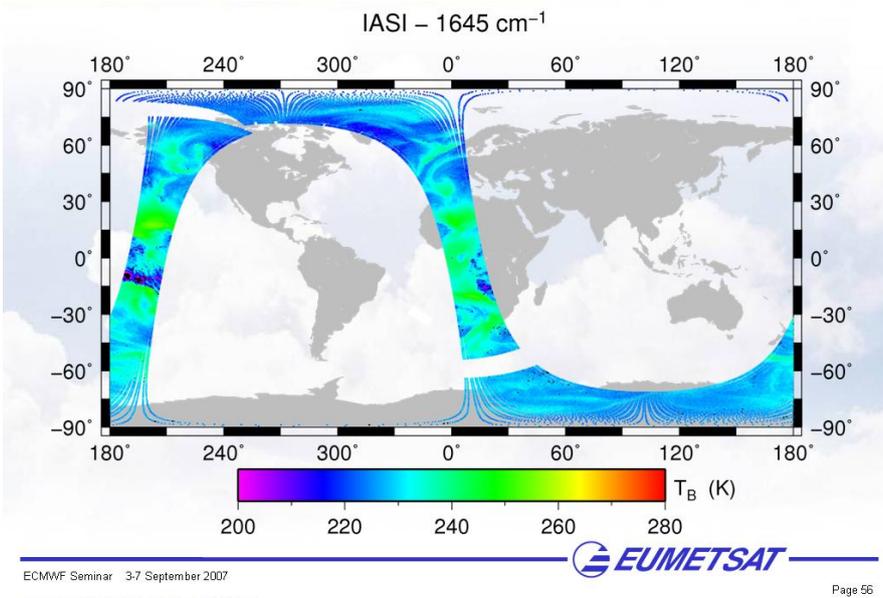


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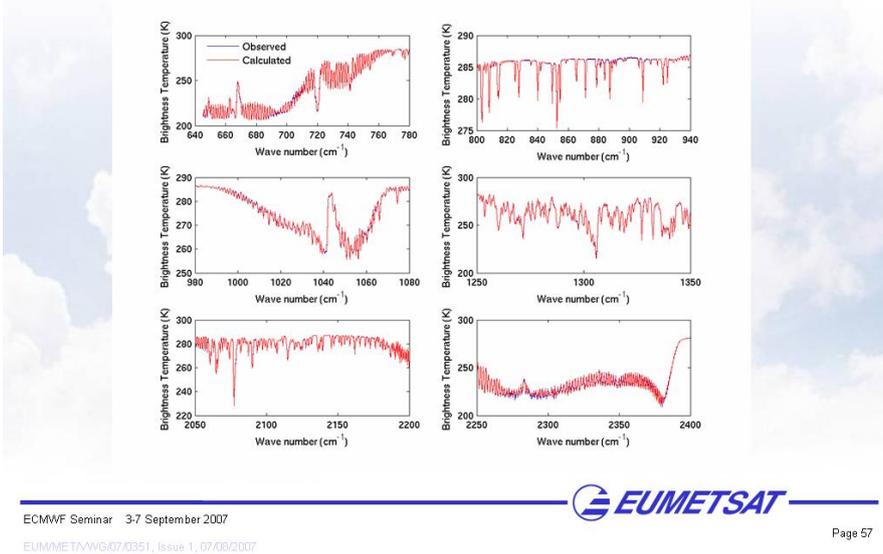


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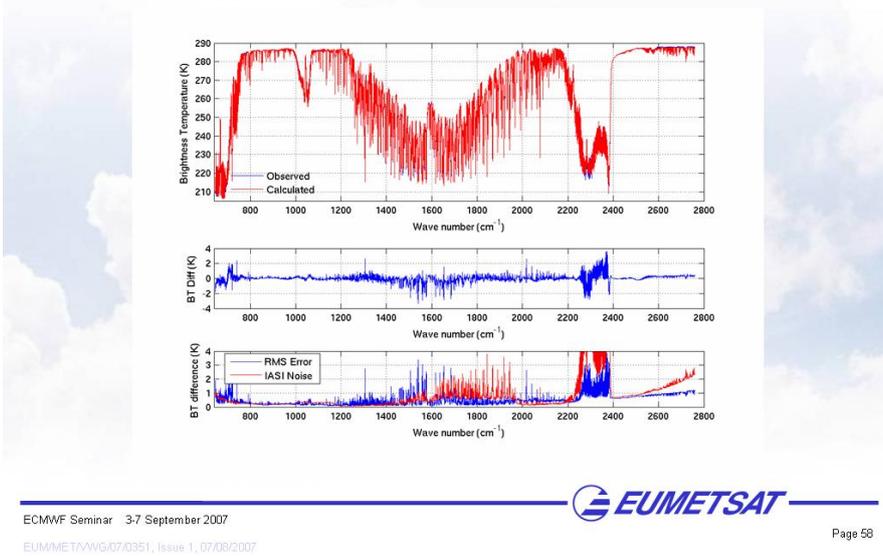
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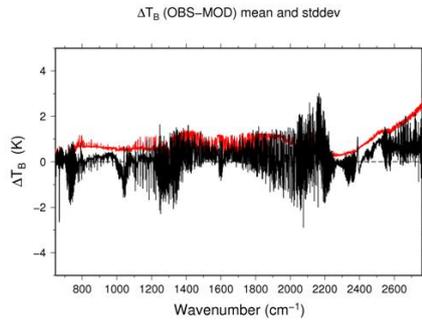
Comparisons of simulated and measured spectra



Comparisons of simulated and measured spectra

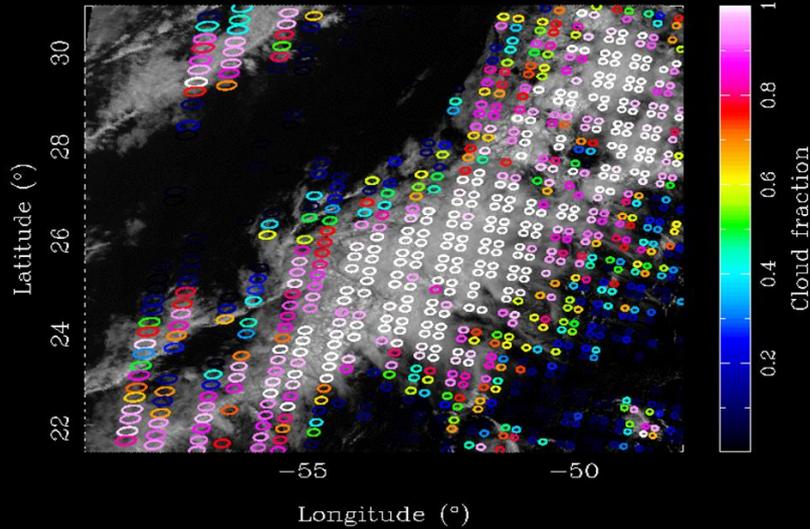


Correction of systematic errors

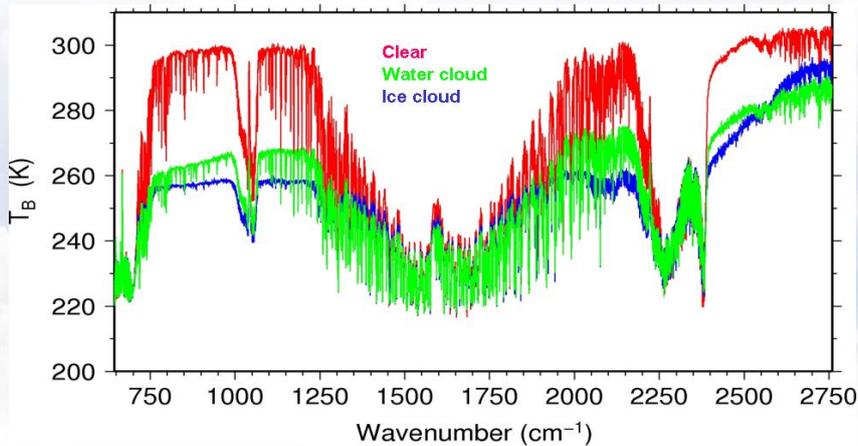


- All retrieval and assimilation schemes use radiative transfer calculations as basis
- Prerequisite for the functionality of the retrieval or assimilation is a good representativity of the measurements by simulated radiances
- Systematic errors:
 - Approximations necessary for fast calculations
 - Insufficient knowledge of spectroscopic data
 - Erroneous input data
- Systematic fit of models to IASI measurements

AVHRR/0.6, cold front, all CFR, IASI 20070418124454Z



Discrimination of ice and water clouds



Geophysical parameters retrieval: state vector to be retrieved

- The state vector to be retrieved consists of the following parameters
 - Temperature profile at a minimum of 40 levels
 - Water vapour profile at a minimum of 20 levels
 - Ozone columns in deep layers (0-6km, 0-12 km, 0-16 km, total column)
 - Land or sea surface temperature
 - Surface emissivity at 12 spectral positions
 - Columnar amounts of N₂O, CO, CH₄, CO₂
 - Cloud amount (up to three cloud formations)
 - Cloud top temperature (up to three cloud formations)
 - Cloud phase
- In case of clouds and elevated surface the state vector has to be modified

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Geophysical parameters retrieval: first retrieval

- Spectra PC scores regression for temperature and water-vapour, and ozone profiles, surface temperature, and surface emissivity
- Artificial neural network (multi-layer perceptron) for trace gases (optionally also for temperature, water-vapour and ozone, depends on configuration setting)
- The results from the first retrieval may constitute the final product or may serve as input to the final, iterative retrieval; the choice depends on configuration setting and on quality of the first retrieval results

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Geophysical parameters retrieval: final, iterative retrieval

- Simultaneous iterative retrieval, seeking maximum probability solution for minimisation of cost function by Marquardt-Levenberg method, using a subset of IASI channels, single or combined to super-channels
- Initialisation with results from first retrieval
- Other choices of initialisation may be selected, depending on configuration setting and availability (e.g. NWP forecast, climatology, ATOVS Level 2 product)
- Background state vector from climatology, ATOVS Level 2 product, adjacent retrieval, or NWP forecast, depending on configuration and availability
- State vector to be iterated depends on cloud conditions and configuration setting (clear, cloudy, variational cloud clearing)

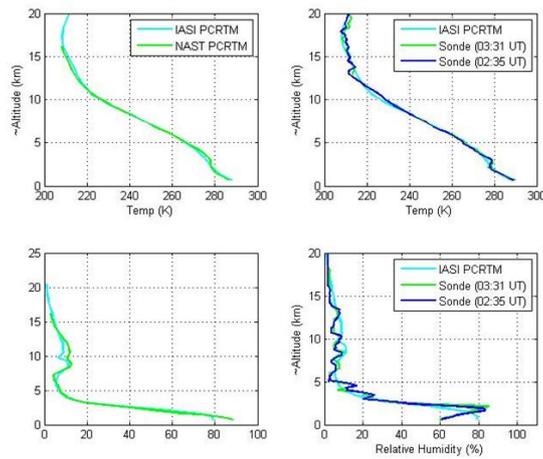
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Comparison: IASI / NAST-I / radiosonde

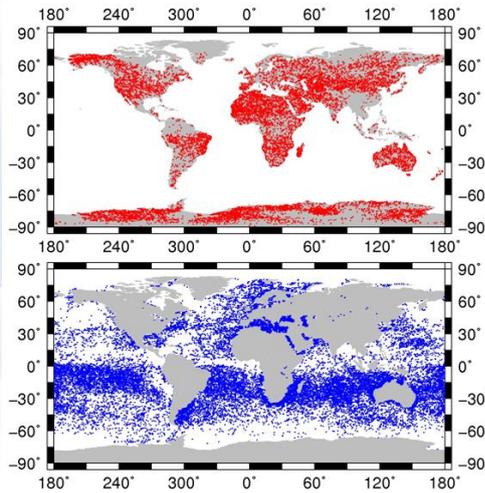


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Comparison: ECMWF / IASI

Clear situations
May - June 2007

Land: 1330 match-ups

Ocean: 21810 match-ups

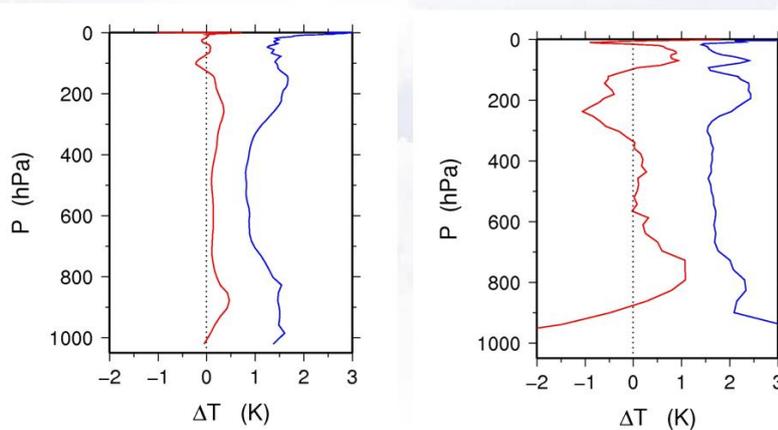
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Comparison: ECMWF - IASI L2



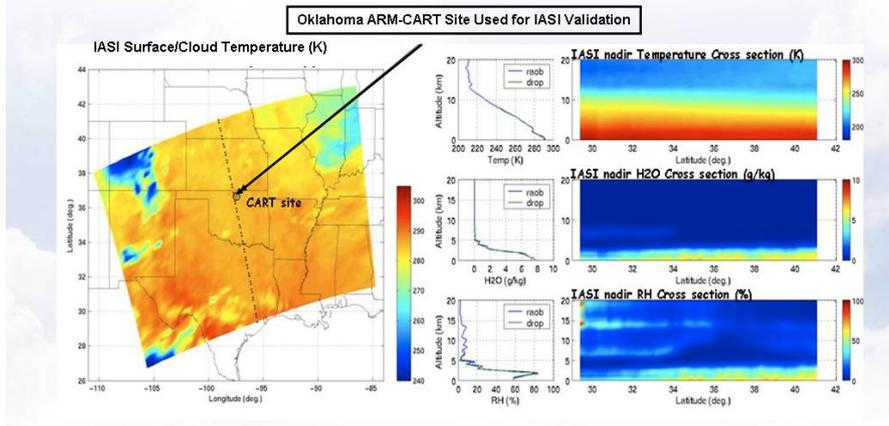
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JAIVEx: Joint Airborne IASI Validation Experiment



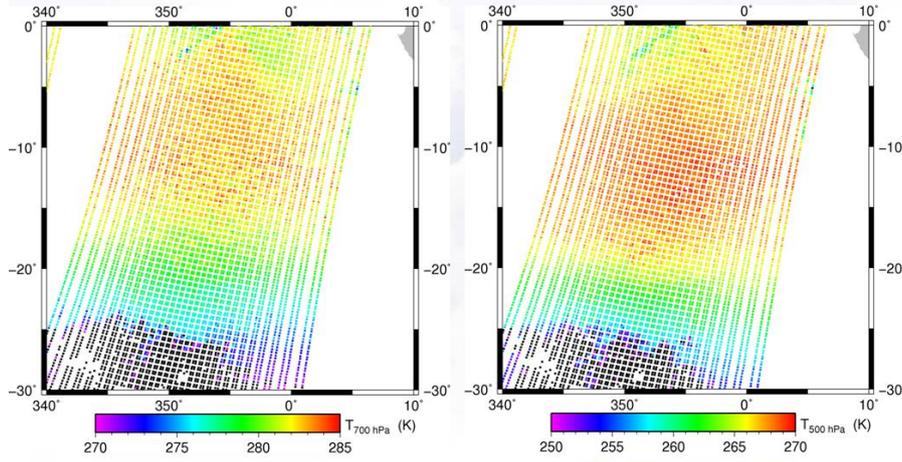
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IASI: temperature retrievals on 10 June 2007 ~09:30 UTC



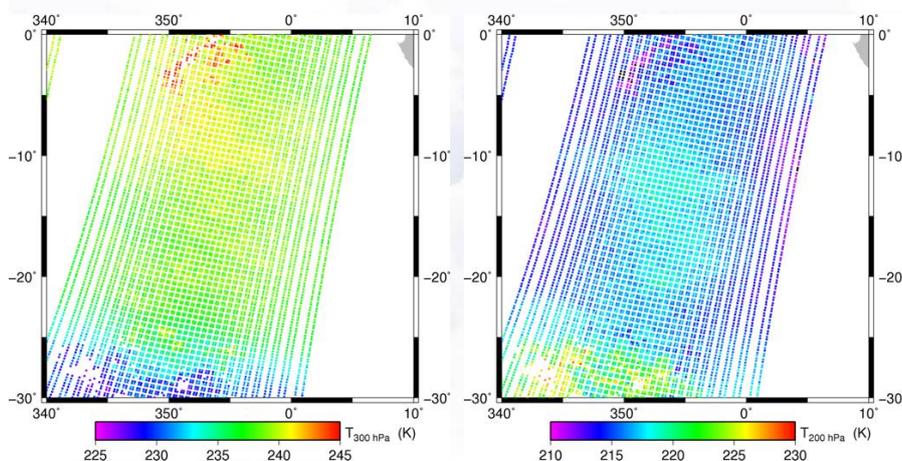
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IASI: temperature retrievals on 10 June 2007 ~09:30 UTC



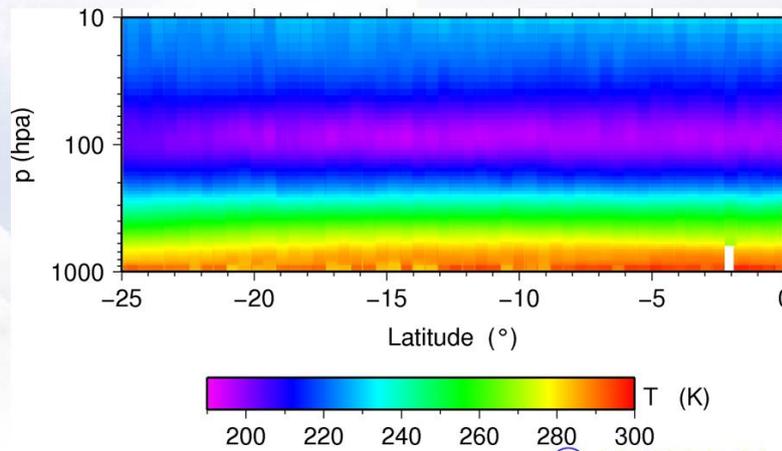
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**IASI: temperature retrievals on 10 June 2007 ~09:30 UTC
cross section along ~7°W**



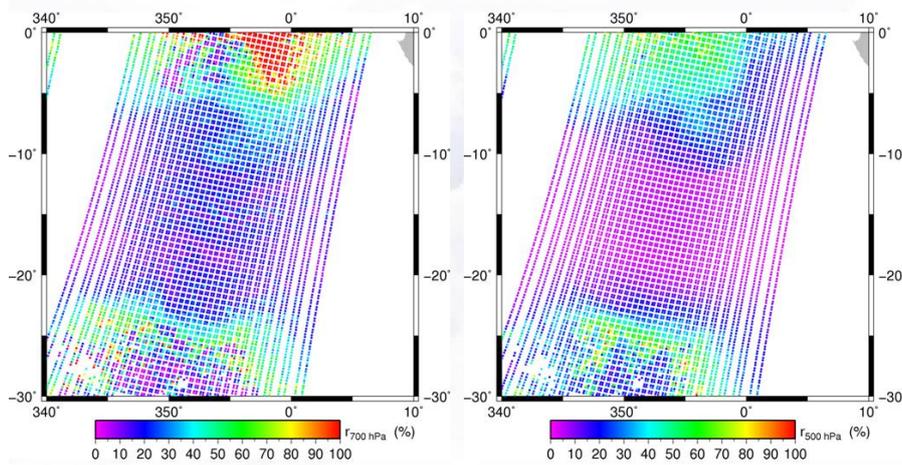
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IASI: humidity retrievals on 10 June 2007 ~09:30 UTC



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IASI level 1 data format

- **Advantages of current data format**
 - User can use the IASI spectra like those from channel radiometers and extract useful parts
 - Interferometric characteristics are hidden from users, e.g. negative radiances
- **Disadvantages of current data format**
 - Large data volume: 2 Mbit/s
 - Quantisation in 16 bit words: slight degradation
 - Full usage of information hardly possible
 - Apodisation of spectra implies non-diagonal error covariances: complication in assimilation and retrieval

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Possible future representation

- **Utilisation of empirical orthogonal functions**
 - Projection of IASI level 1A spectra (unapodised) on ~250 EOFs
 - Dissemination of EOF-scores
- **Advantage and new potential**
 - Data volume: 49 kbit/s
 - Re-constructed spectra are quasi noise-free
 - Direct assimilation of EOF scores instead of radiance spectra

Conclusion

- **Metop-A has been launched and been operated successfully**
- **New instruments have been successfully commissioned**
- **Level 1 data are routinely disseminated to users**
- **Validation of the numerous products is ongoing**

PCRTM: radiative transfer in EOF-space

- PCRTM calculates EOF-scores (Y) instead of spectral radiances (R)

$$\vec{Y} = U \times \vec{R}^{mono}$$

$$\frac{\partial Y_i}{\partial X} = \sum_{l=1}^{N_{mono}} a_l \frac{\partial R^{mono}(l)}{\partial X}$$

- Relationship between EOF scores and measured radiances:

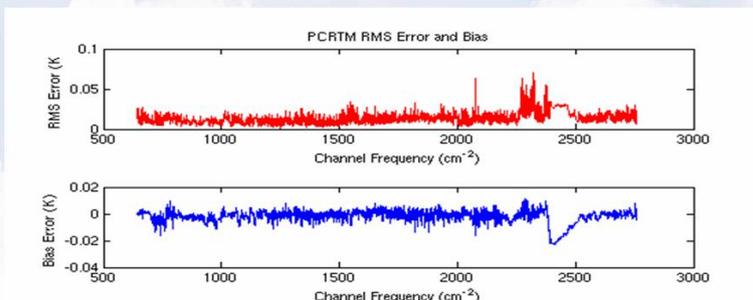
$$\bar{R}_i^{chan} = \frac{\sum_{k=1}^N \phi_k R_k^{mono}}{\sum_{k=1}^N \phi_k}; \quad \vec{Y} = U^T \times \vec{R}^{chan}$$

- Spectral radiances can be calculated from EOFs and corresponding scores:

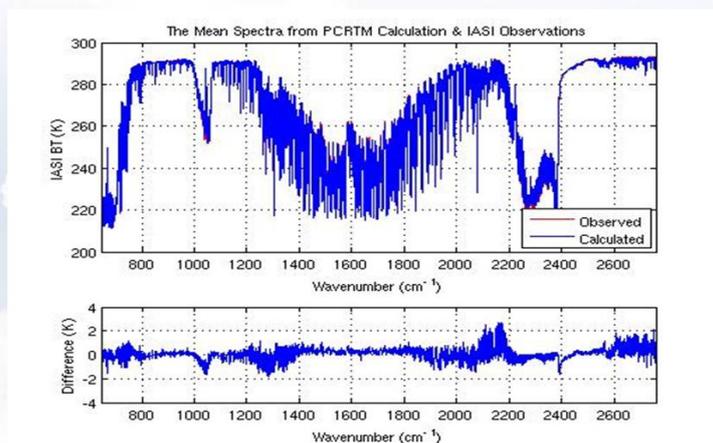
$$\vec{R}^{chan} = U \times \vec{Y} = \sum_{i=1}^{N_{EOF}} y_i \vec{U}_i + \vec{\epsilon}$$

PCRTM: Training with LBL-model

- RMS error in brightness temperature: < 0.025 K
- Systematic errors in brightness temperature: (-0.0002 K, 0.0004 K)



PCRTM: validation with ECMWF and IASI data



PCRTM-retrieval: Levenberg-Marquardt-iteration

$$X_{n+1} - X_n = (K^T S_y^{-1} K + \lambda I + S_x^{-1})^{-1} K^T S_y^{-1} [(Y_n - Y_m) + K(X_n - X_n)]$$

50 retrieved EOF-Scores:

- Surface temperature: 1
- Temperature profile: 19
- Humidity profile: 15
- Ozone profile: 10
- Emissivity: 5

Variable	Radiance/state vector: dimensions	EOF-space: dimensions
Y	8461	100
X	>100	50
K	> 8461x100	100x50
S_y^{-1}	8461x8461	100x100
S_x	> 100x100	50x50
Calculation of K and Y	~2 s	~0.1 s