



## *The ICON project:*

*Design and performance of an unstructured grid approach for a global triangular grid model*

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*Max Planck Institute for Meteorology*





# ICON : ICOsahedral, Nonhydrostatic model NWP + Climate + Chemistry

- **ICON development team:**  
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# Outline

- Overview of the **ICON** development project:  
motivations and project goals
- Model **equations** and **discretization** approach
- Preliminary results of a **shallow water** model
- Outlook on future work





## Desired features for a new model

- Unique framework for large/small scale, lower/upper atmospheric dynamics
- Consistency between discrete tracer advection and discrete continuity equation
- Mass conservative static local grid refinement without spurious interface effects: building block for a multiscale model





# Concept of discretization approach

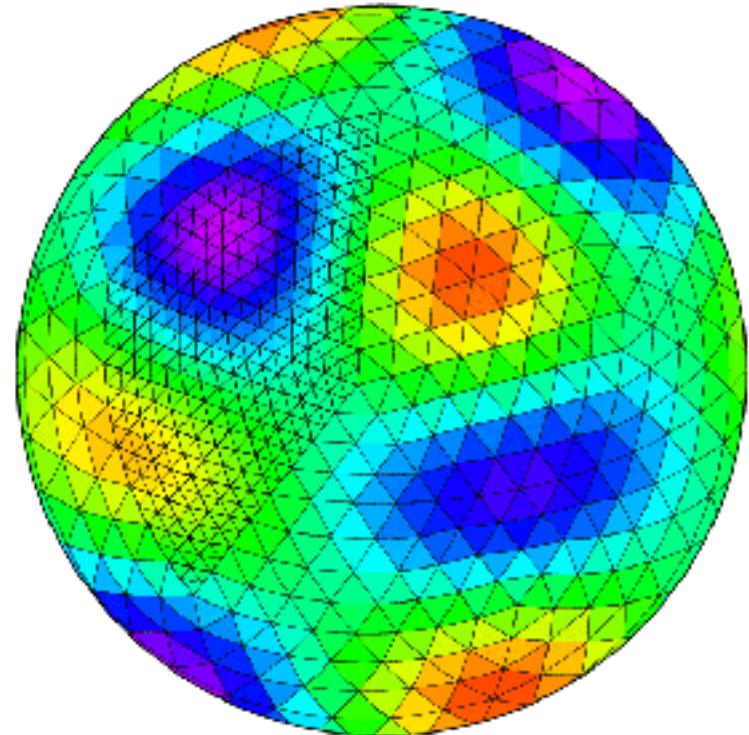
- Achieve the same **accuracy** and **efficiency** as advanced **NWP** models...
- ... but preserve some **discrete** equivalents of **global** invariants relevant to geophysical flow...
- ... and narrow the **gap** to Computational Fluid Dynamics (**CFD**) models.





# Geodesic icosahedral grids

- Special case of **Delaunay** triangulation
- Solve the **pole** problem



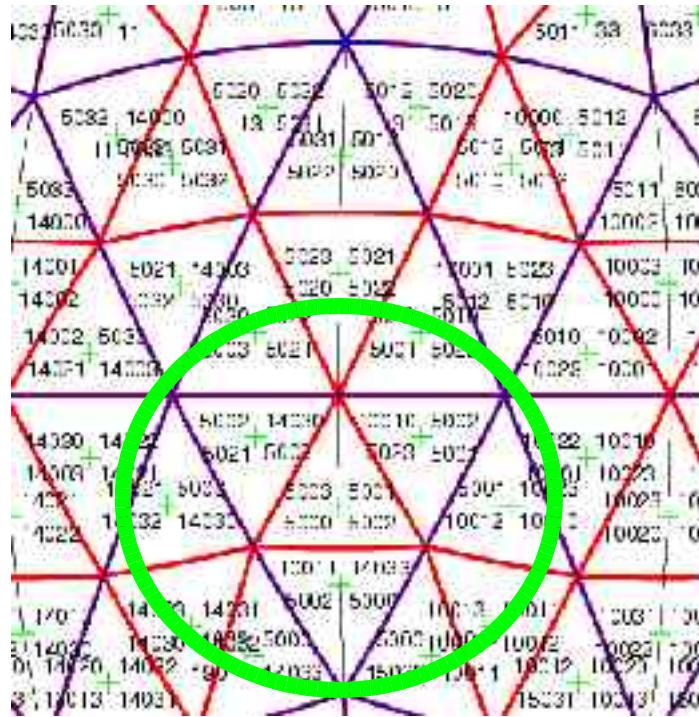
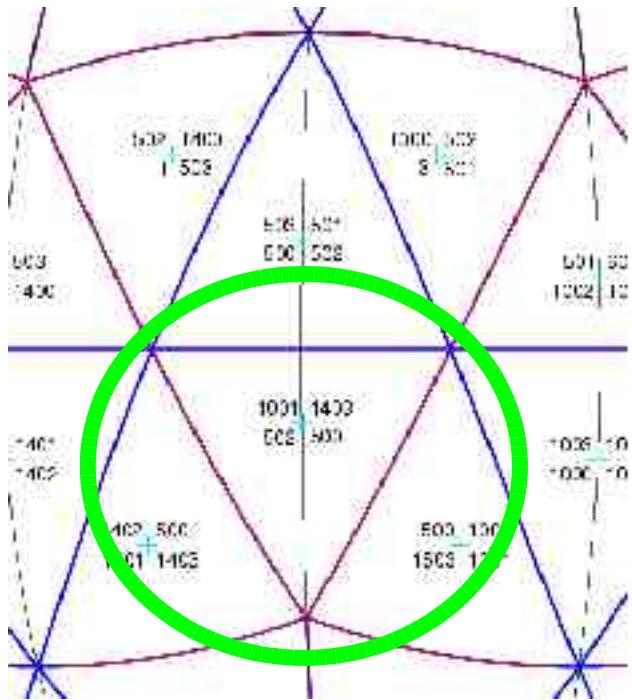
- Local grid refinement
- Multiscale modelling





# Implementation issues

Indirect addressing that preserves **data locality**



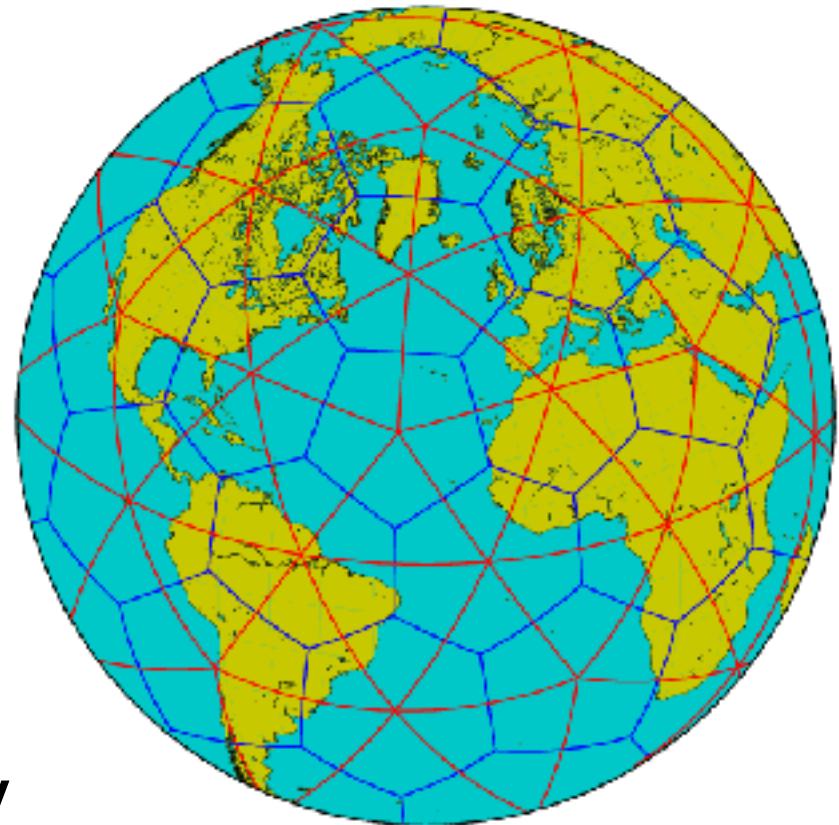
Parallelization: horizontal data decomposition





# Spatial discretization

- Finite volume discretization with **triangular** control volumes:  
**triangular C grid**
- Delaunay -Voronoi property





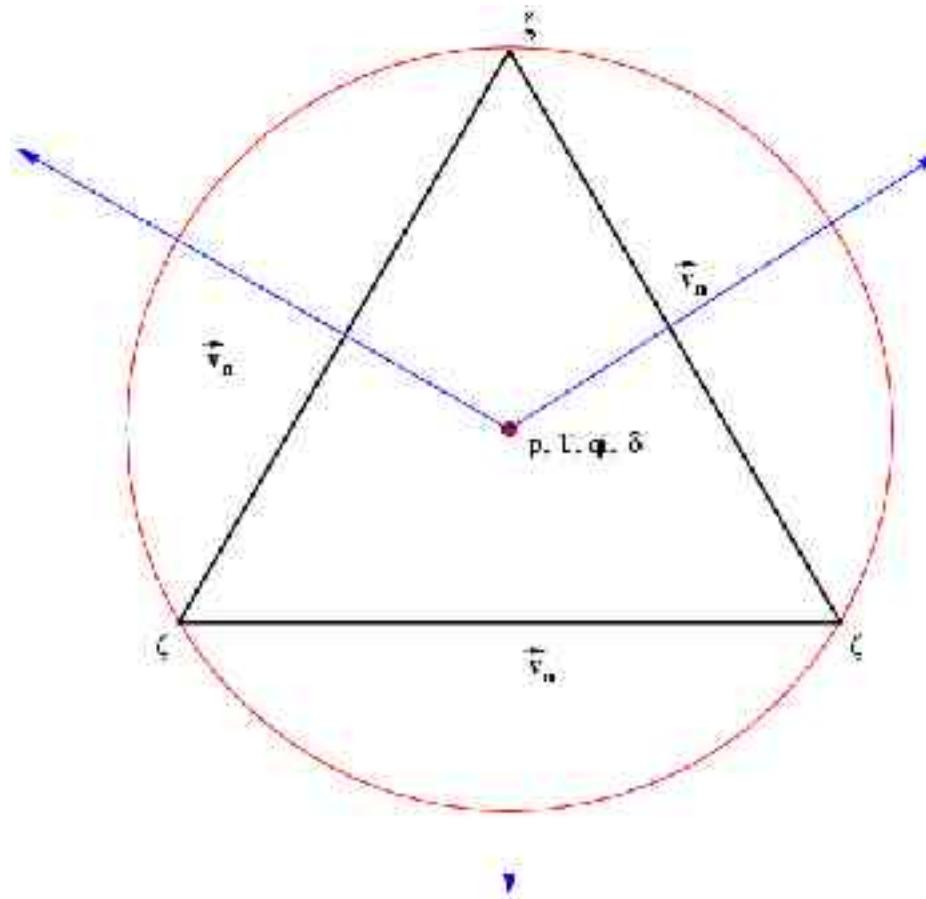
## Spatial discretization, properties

- Vorticity at triangle **vertices**: discrete **Helmholtz** decomposition (Nicolaides 1992)
- No **spurious vorticity production**
- Raviart-Thomas reconstruction of velocity, **average** onto edge for tangential component
- Improve Raviart-Thomas reconstruction by **Radial basic functions** giving higher order accuracy



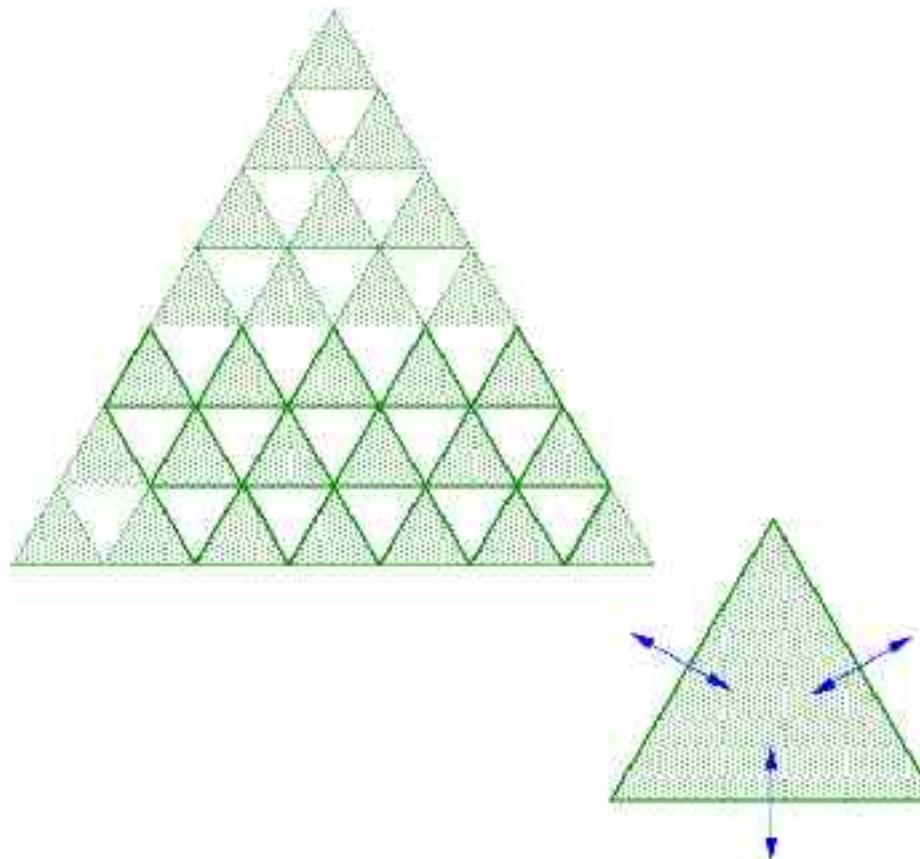


# The structure of a gridpoint





# Some ideas on parallelization





# A datastructure

```
TYPE grid_element
  INTEGER :: index
  INTEGER :: parent_index
  INTEGER :: child_index(4)
  INTEGER :: neighbor_index(3)
  TYPE(cartesian_coordinates) :: center
  REAL(dp) :: area
  TYPE(cartesian_coordinates) :: vertex(3)
  TYPE(cartesian_coordinates) :: edge_center(3)
  TYPE(cartesian_coordinates) :: edge_normal(3)
  REAL(dp) :: primal_edge_length(3)
  REAL(dp) :: dual_edge_length(3)
END TYPE grid_element
```

```
TYPE grid
  INTEGER :: level
  TYPE(grid_element), POINTER :: g(:)
END TYPE grid
```

SX-6: 2.2 Gflops for PCG

Cache-based architectures:  
unusable





## ... more on data structures

INTEGER, ALLOCATABLE :: index(:)

INTEGER, ALLOCATABLE :: parent\_index(:)

INTEGER, ALLOCATABLE :: child\_index(:,::)

INTEGER, ALLOCATABLE :: neighbor\_index(:,::)

REAL(dp), ALLOCATABLE :: area(:)

REAL(dp), ALLOCATABLE :: edge\_primal(:,::)

REAL(dp), ALLOCATABLE :: edge\_dual(:,::)

REAL(dp), ALLOCATABLE :: center(:,::)

REAL(dp), ALLOCATABLE :: vertex(:,::,:)

REAL(dp), ALLOCATABLE :: edge\_center(:,::,:)

REAL(dp), ALLOCATABLE :: edge\_normal(:,::,:)

Acceptable solution:  
but not well structured





# ... even more on data structures

TYPE triangle

```
TYPE(triangle), POINTER :: parent
TYPE(triangle), POINTER :: sub_triangle0 => NULL()
TYPE(triangle), POINTER :: sub_triangle1 => NULL()
TYPE(triangle), POINTER :: sub_triangle2 => NULL()
TYPE(triangle), POINTER :: sub_triangle3 => NULL()
TYPE(triangle), POINTER :: neighbor0 => NULL()
TYPE(triangle), POINTER :: neighbor1 => NULL()
TYPE(triangle), POINTER :: neighbor2 => NULL()
TYPE(edge), POINTER :: edge0 => NULL()
TYPE(edge), POINTER :: edge1 => NULL()
TYPE(edge), POINTER :: edge2 => NULL()
TYPE(vertex), POINTER :: vertex0 => NULL()
TYPE(vertex), POINTER :: vertex1 => NULL()
TYPE(vertex), POINTER :: vertex2 => NULL()
END TYPE triangle
```

Topological point  
of view





# Discrete wave dispersion analysis

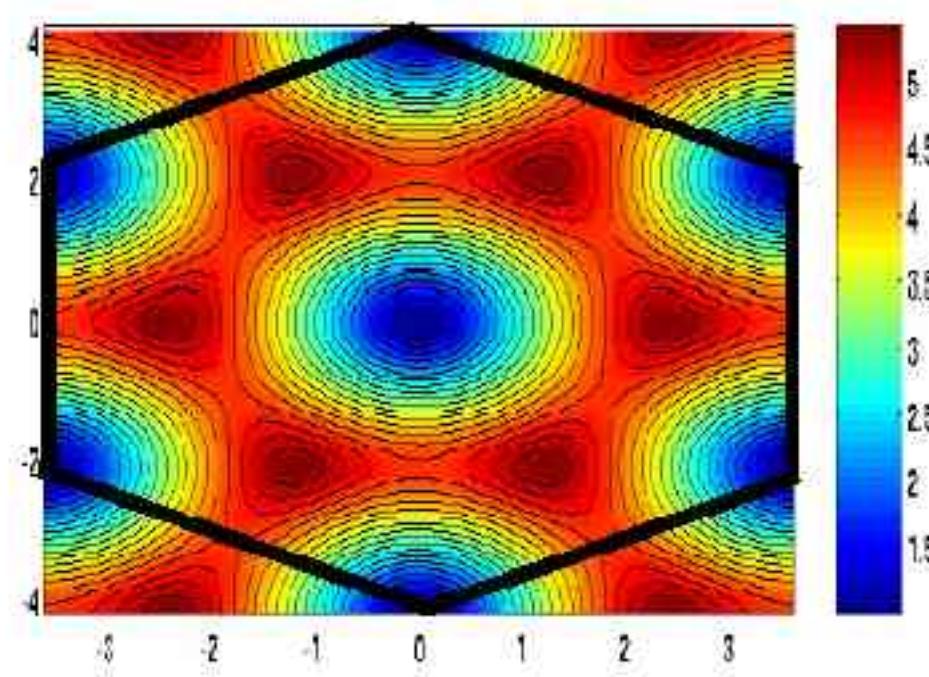
- **Stationary** geostrophic solution, no spurious pressure modes
- Two **physical** gravity wave modes
- Two **spurious** gravity wave modes: frequencies always **higher** than physical ones

$$\omega^2 = \frac{8gH}{d^2} \pm \frac{8gH}{3d^2} \sqrt{1 + 4\cos^2\left(\frac{\sqrt{3}}{2}kd\right) + 4\cos\left(\frac{\sqrt{3}}{2}kd\right)\sin\left($$





# Dispersion plot, physical mode



- Less **good** wavenumber space than quadrilateral C-grid
- Zero **group velocity** at high wavenumbers





# Discrete global invariants

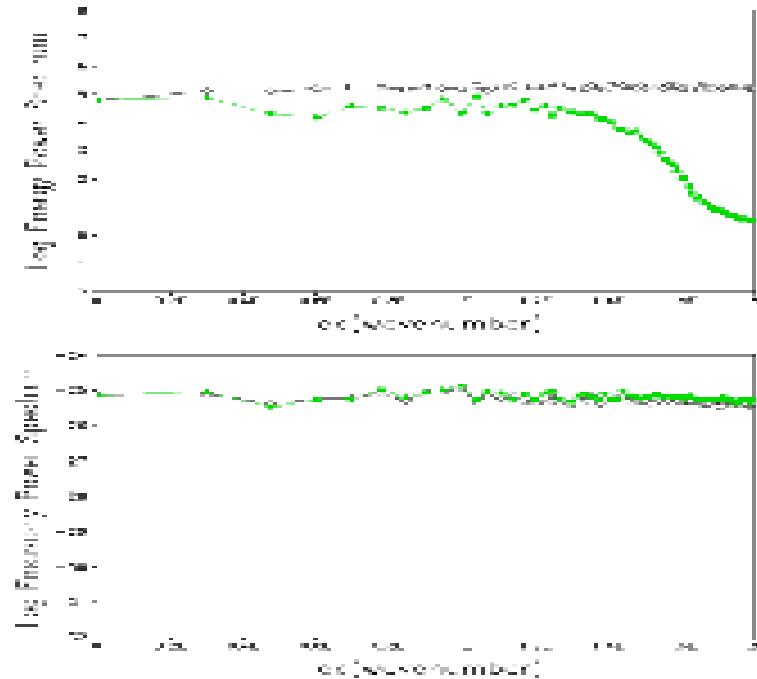
- Mass conservation, **consistent discretizations** of continuity equation and tracer transport
- Mass and potential vorticity conservation, **no spurious vorticity production**
- Potential **enstrophy** conserving variant
- **Energy** conserving variant: Sadourny, JAS 1975





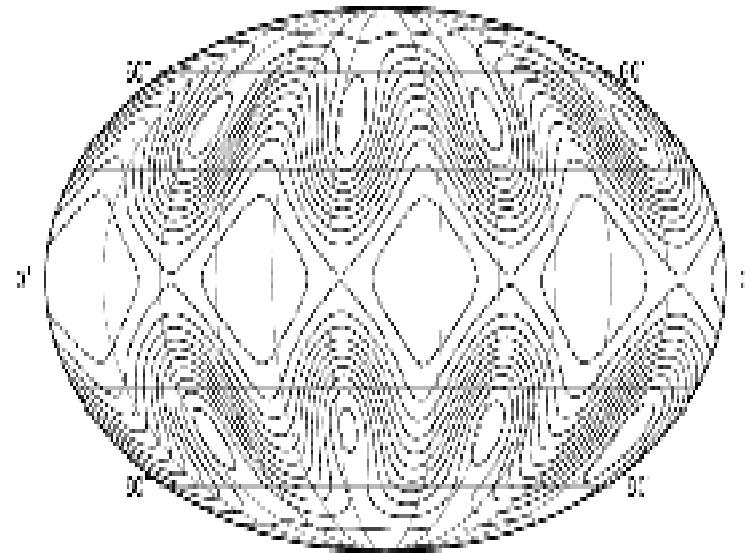
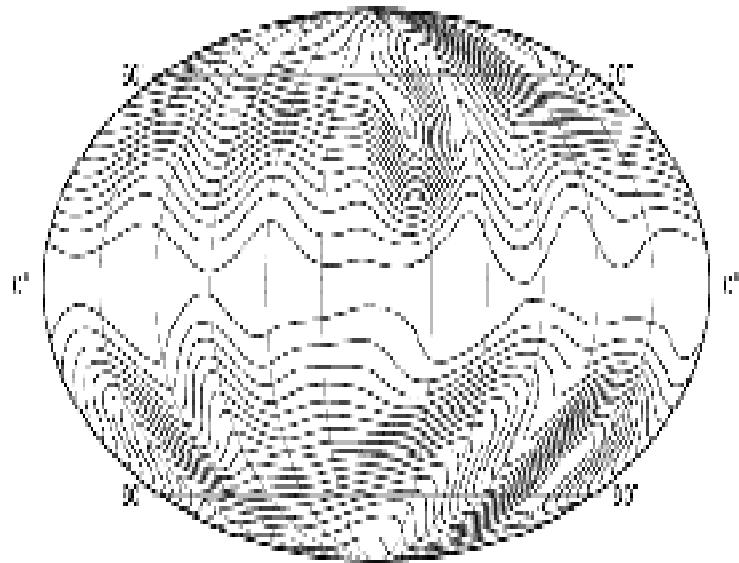
# Random initial data on rotating plane (1000 days)

Relative vorticity after 1000 days integration with random initial data (numerical test carried out by Todd Ringler, CSU)





# Shallow water test cases: tests 5-6





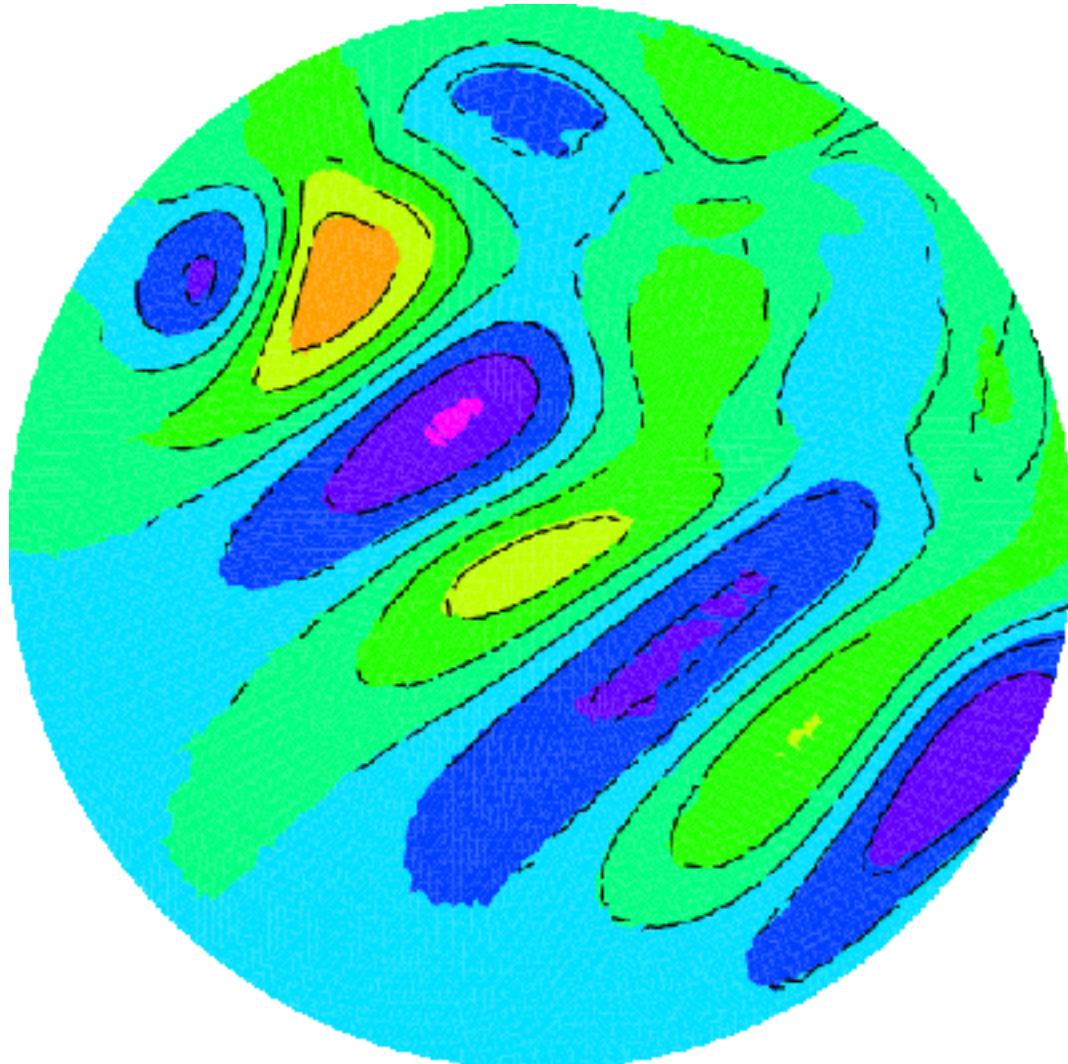
# Test case 5

## Relative vorticity

### day 10

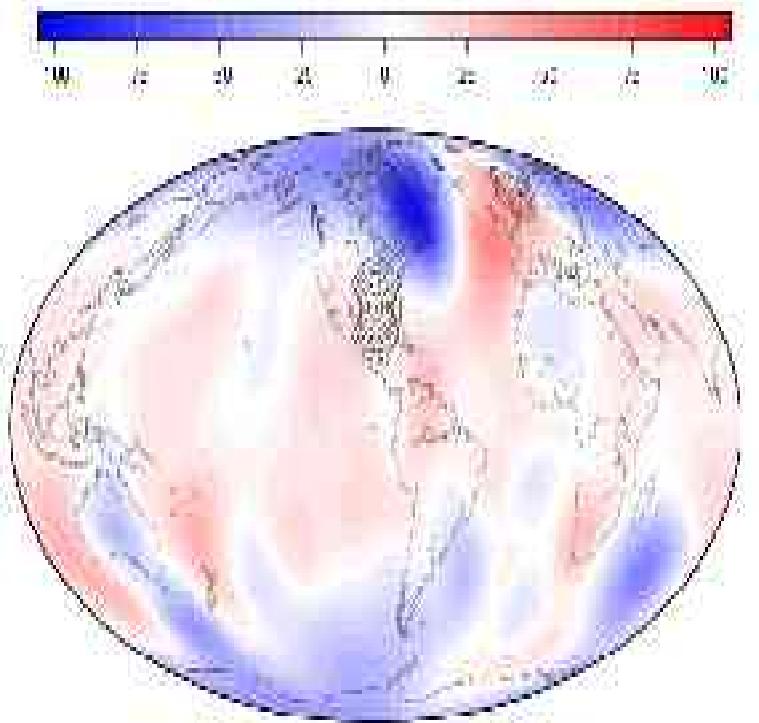
Colour shading:  
model results

Black contours:  
NCAR reference  
spectral model

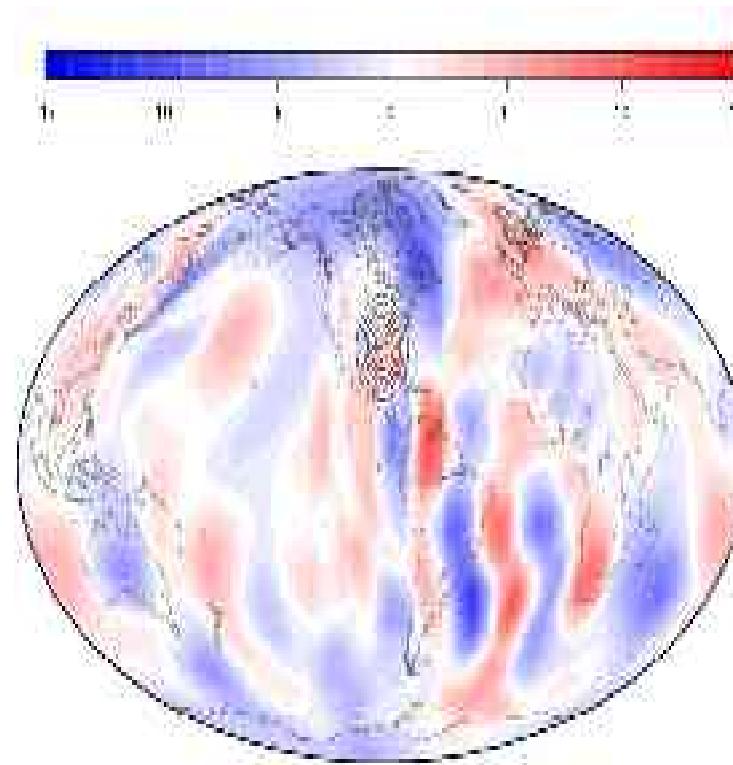




## Test 5, height field error at day 15



Glevel 6,  $dt = 900$  s



Glevel 7,  $dt = 90$  s





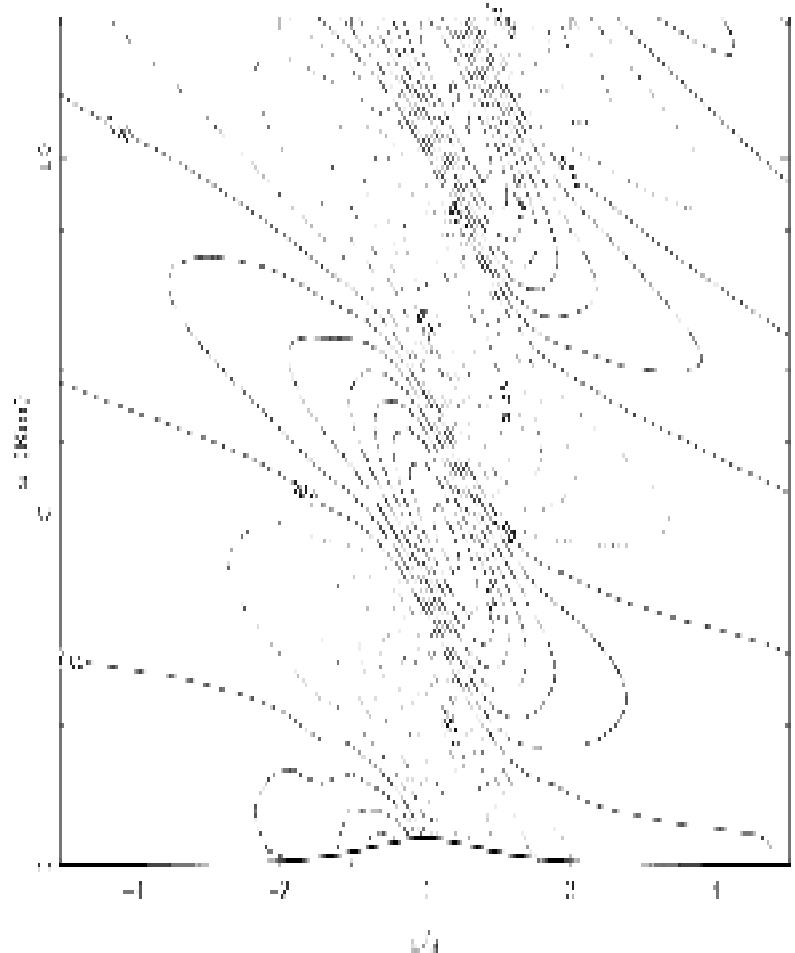
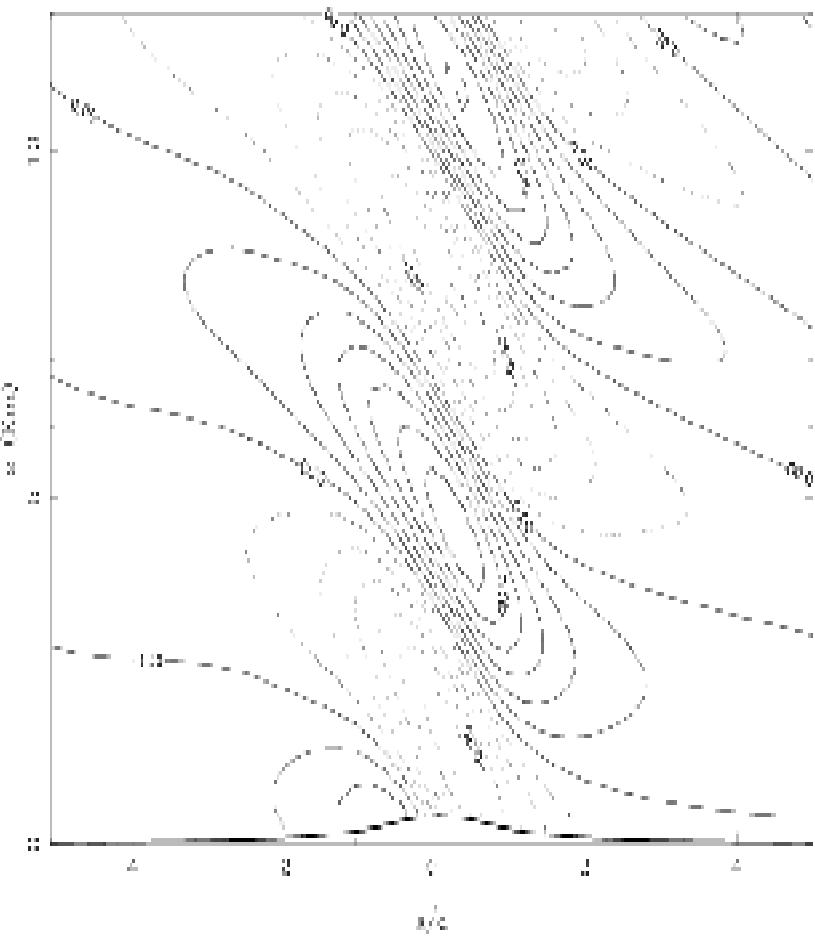
## Some options for vertical coordinates

- **Hybrid pressure** vertical coordinate + new horizontal discretization: preliminary 3d-ICON model
- **Terrain following** normalized height coordinate + new horizontal discretization: first choice for operational, global nonhydrostatic model
- Non normalized, **geometric height coordinate + cut cells**





# Geometric height + cut cells





# Outlook

- Optimized data structure and parallelization for model on **locally refined grids**
- **Hydrostatic, 3D model on locally refined grids**
- Coupling to **existing MPI** physics package, impact of **spurious modes** on simulations with full physics
- **Sensitivity** of results to local refinement

